

1. For the function $\text{Bel}: 2^X \rightarrow [0,1]$ find the basic probability assignment $m: 2^X \rightarrow [0,1]$ and the plausibility function $\text{Pl}: 2^X \rightarrow [0,1]$ where $X=\{0,1,2,3\}$ and $\text{Bel}(\{0\}) = \text{Bel}(\{1\})=0$, $\text{Bel}(\{2\}) = \text{Bel}(\{3\}) = \text{Bel}(\{0,2\}) = \text{Bel}(\{0,3\}) = \text{Bel}(\{1,2\}) = \text{Bel}(\{1,3\}) = \frac{1}{4}$, $\text{Bel}(\{0,1\}) = \text{Bel}(\{2,3\}) = \text{Bel}(\{0,2,3\}) = \text{Bel}(\{1,2,3\}) = \frac{1}{2}$, $\text{Bel}(\{0,1,2\}) = \text{Bel}(\{0,1,3\}) = \frac{3}{4}$.
2. For the function $\text{Bel}: 2^X \rightarrow [0,1]$ find the basic probability assignment $m: 2^X \rightarrow [0,1]$ and the plausibility function $\text{Pl}: 2^X \rightarrow [0,1]$ where $X=\{1,2,3\}$ and $\text{Bel}(\{1\}) = \text{Bel}(\{2\})=0$, $\text{Bel}(\{3\}) = \text{Bel}(\{1,3\}) = \frac{1}{2}$, $\text{Bel}(\{1,2\}) = \frac{1}{4}$, $\text{Bel}(\{2,3\}) = \frac{3}{4}$.

3. $X=\{x_1, x_2, x_3, x_4, x_5\}$, and two basic probability assignments, m and n are given below:

| | $\{x_4, x_5\}$ | $\{x_1, x_3\}$ | $\{x_1, x_2\}$ | $\{x_2, x_4\}$ | $\{x_1, x_2, x_3\}$ |
|-----|----------------|----------------|----------------|----------------|---------------------|
| m | $\frac{3}{8}$ | $\frac{3}{8}$ | $\frac{1}{4}$ | 0 | 0 |
| n | 0 | 0 | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{2}$ |

Assuming independence of both pieces of evidence, find their orthogonal sum $m \oplus n$.

4. $X=\{a, b, c\}$, and two basic probability assignments, m and n are given below:

| | $\{a\}$ | $\{b\}$ | $\{c\}$ | $\{a, b\}$ | $\{a, c\}$ | $\{b, c\}$ | $\{a, b, c\}$ |
|-----|---------|---------|---------|------------|------------|------------|---------------|
| m | 0.3 | 0 | 0.2 | 0.3 | 0 | 0.1 | 0.1 |
| n | 0 | 0 | 0.2 | 0.2 | 0.3 | 0.2 | 0.1 |

Assuming independence of both pieces of evidence, find their orthogonal sum $m \oplus n$.

5. Assume that $S=(X, A, V)$ is an information system given below:

| | A | B |
|-------|---|---|
| x_1 | 1 | 2 |
| x_2 | 1 | 1 |
| x_3 | | 1 |
| x_4 | 2 | |
| x_5 | | 2 |

Propose two different interpretations of attributes A, B by belief functions and by plausibility function.