

$\hat{y}_n = +1, y_n = -1 \rightarrow$  false positive (FP) mistake.

$\hat{y}_n = -1, y_n = +1 \rightarrow$  false negative (FN) mistake.

Q: Will the updated  $w$  do "better" on the example  $x_n$  that it previously misclassified?

Vector difference  $w - x \rightarrow w$

~~for  $i$  in range( $w$ .shape[0]):  
 $w[i] = w[i] - x[i]$~~

vectorized version  
 $w = w - x$

Normally, training set is shuffled between epochs.

Perceptron update rule: if  $\underbrace{w^T x_n}_{h_n} \cdot t_n \leq 0$   
 $w = w + \eta t_n x_n$

Q: Let  $w^{(1)}$  be the params. obtained when  $\eta = 1$   
 $w^{(2)}$  ———— when  $\eta = 2$ .  $\rightarrow$  Train Perceptron to get them.

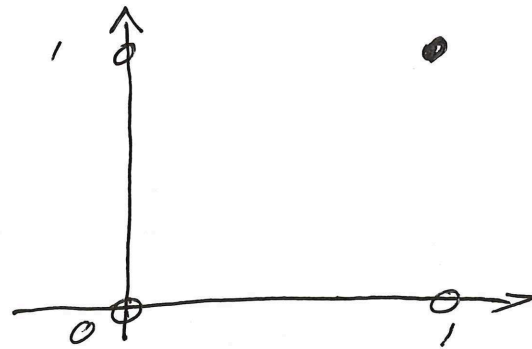
Let  $x$  be some arbitrary example.

$$w^{(2)} x = 2 w^{(1)} x$$

$$\begin{aligned} \text{if } w^{(1)} x \geq 0 &\rightarrow w^{(2)} x \geq 0 \\ w^{(1)} x < 0 &\rightarrow w^{(2)} x < 0. \end{aligned}$$

$$X = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix}$$

$$y = [-1, -1, -1, +1]$$



add bias feature  
to each feature vector

use column-stack in np.

$$\begin{bmatrix} 1 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

$w_0$   $w_1$   $w_2$

def train(x, y):

$$w = 0$$

⋮  
⋮  
⋮

return w