## Assignment 7

## Oral questions

No oral questions assigned due to the upcoming midterm.

## Questions to be answered in writing

Questions 1 and 2 are about Hyperbolic Geometry, the last question is about Euclidean Geometry.

1. Prove Theorem 8.7.
2. Assume that the lines $\ell$ and $\ell^{\prime}$ have a common perpendicular line segment $M M^{\prime}$. Prove that $M M^{\prime}$ is the shortest segment between any point of $\ell$ and any point of $\ell^{\prime}$. (Hint: Assume $A \in \ell, A^{\prime} \in \ell^{\prime}$ and compare $A A^{\prime}$ to $M M^{\prime}$. Use the written exercise of Assignment 6 when $A A^{\prime}$ is perpendicular to $\ell$ and then use the third oral exercise of Assignment 6 in the other case.)
3. Use the picture below to find an exact formula for $\cos \left(72^{\circ}\right)=x / 2$.


Prove your claim using similarity of triangles and the angle bisector theorem.

