## Assignment 9

## Oral questions

1. $5.5 / 11$
2. $5.5 / 12$

## Questions to be answered in writing

1. Let $A B D C$ be a quadrilateral whose base angles $\angle A$ and $\angle B$ are right angles. Prove that if $A C<B D$ then $\angle D<\angle C$. (Hint: Choose $E$ between $B$ and $D$ on the line $B D$ such that $A C=B E$. Apply Theorem 3.6.4 and the weak exterior angle theorem. You are allowed to use without proof the fact that $E$ is interior to $\angle A C D$.)
2. Assume that the lines $\ell$ and $\ell^{\prime}$ have a common perpendicular line segment $M M^{\prime}$. Prove that $M M^{\prime}$ is the shortest segment between any point of $\ell$ and any point of $\ell^{\prime}$. (Hint: Assume $A \in \ell, A^{\prime} \in \ell^{\prime}$ and compare $A A^{\prime}$ to $M M^{\prime}$. Use the previous written exercise when $A A^{\prime}$ is perpendicular to $\ell$ and then use the first oral exercise from Assignment 4 in the other case.)
