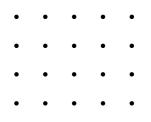
Target Practice 1

1. Two points are simultaneously and randomly selected from a 4×5 grid of 20 lattice points. What is the probability that the distance between them is $\sqrt{5}$? Express your answer as a fraction.



- 2. In triangle ABC, the measures of $\angle A$, $\angle B$, and $\angle C$ form an arithmetic sequence. If $\angle A$ is exactly half as big as $\angle C$, what is number of degrees in $\angle C$?
- 3. A rectangular box has dimensions 5 inches by 7 inches by 11 inches. Two bugs are at opposite corners of the box, as far away from one another as possible. To the nearest integer, how far apart are they?
- 4. The sum of two numbers is 7 and their product is 8. Find the sum of their reciprocals.
- 5. How many noncongruent acute triangles have integer sides and perimeter 12?
- 6. A cube has edges of length 6 units. What is the distance from the midpoint of a face diagonal to the vertex farthest away? Leave your answer in simplest radical form.
- 7. If x + y = 3 and xy = 1, what is $x^3 + y^3$?
- 8. The number 75 is expressible as a sum of four numbers a, b, c, and d in such a way that the same number results when 4 is added to a, when 4 is subtracted from b, when 4 is multiplied by c, and when 4 is divided into d. Find a, b, c, and d.
- 9. Suppose r is a positive root of $x^2 7x = 1$. Find the distance between r and its reciprocal.
- 10. What is the total number of rectangles of all sizes in the diagram?

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