

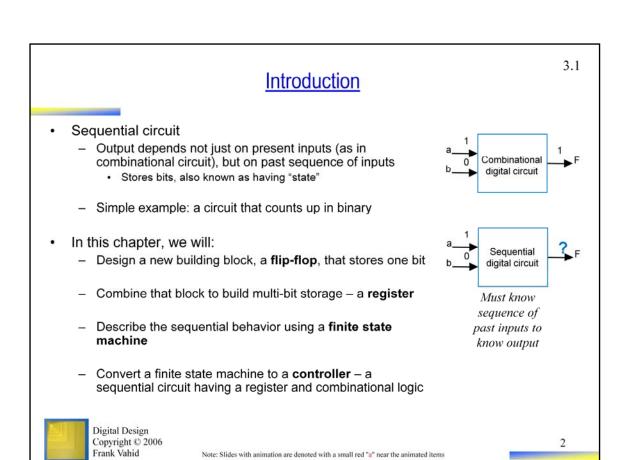
Digital Design

Chapter 3: Sequential Logic Design -- Controllers

Slides to accompany the textbook Digital Design, First Edition, by Frank Vahid, John Wiley and Sons Publishers, 2007. http://www.ddvahid.com

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Note: Slides with animation are denoted with a small red "a" near the animated items

Example Needing Bit Storage

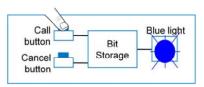
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- Flight attendant call button
 - Press call: light turns on
 - · Stays on after button released
 - Press cancel: light turns off
 - Logic gate circuit to implement this?

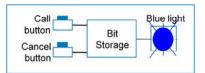


Doesn't work. Q=1 when Call=1, but doesn't stay 1 when Call returns to 0

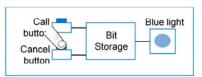
Need some form of "feedback" in the circuit



1. Call button pressed - light turns on

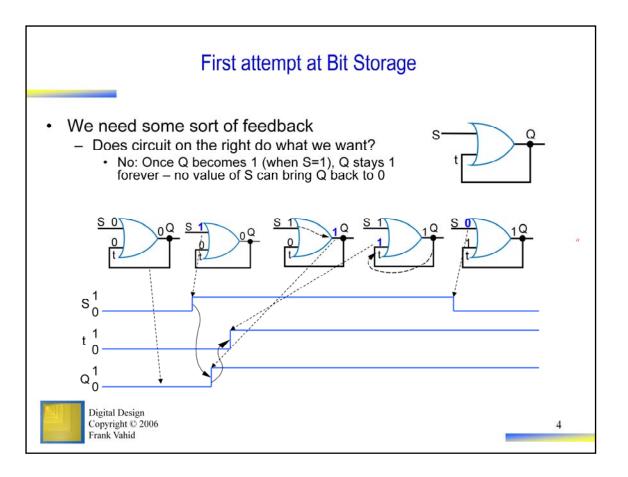


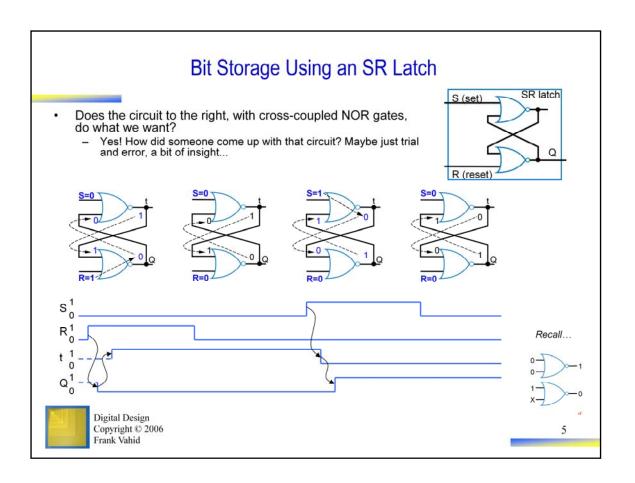
2. Call button released - light stays on



3. Cancel button pressed - light turns off



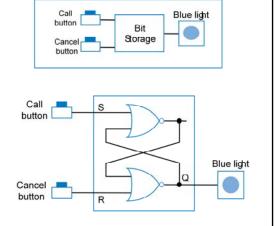




Example Using SR Latch for Bit Storage

- SR latch can serve as bit storage in previous example of flight-attendant call button
 - Call=1: sets Q to 1
 - Q stays 1 even after Call=0
 - Cancel=1 : resets Q to 0

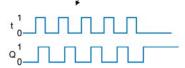
· But, there's a problem...





Problem with SR Latch If S=1 and R=1 simultaneously, we don't know what value Q will take

Q may oscillate. Then, because one path will be slightly longer than the other, Q will eventually settle to 1 or 0 – but we don't know which.

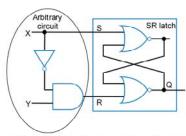




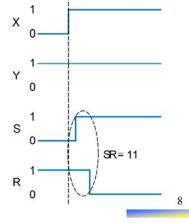
Problem

Problem with SR Latch

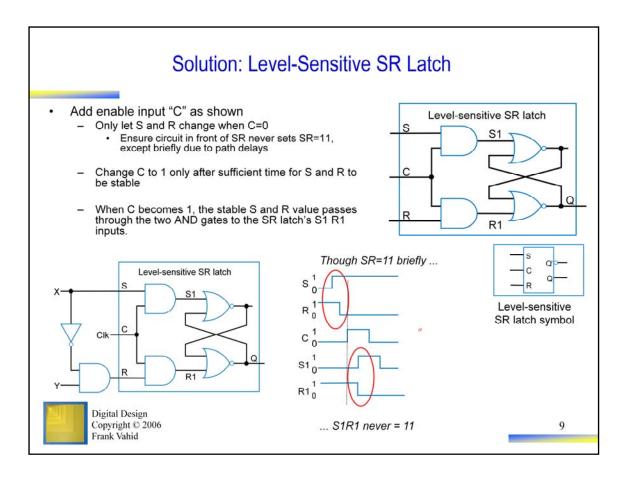
- Problem not just one of a user pressing two buttons at same time
- Can also occur even if SR inputs come from a circuit that supposedly never sets S=1 and R=1 at same time
 - But does, due to different delays of different paths



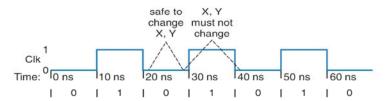
The longer path from X to R than to S causes SR=11 for short time – could be long enough to cause oscillation







Clock Signals for a Latch



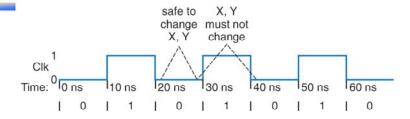
- · How do we know when it's safe to set C=1?
 - Most common solution -make C pulse up/down
 - . C=0: Safe to change X, Y
 - C=1: Must not change X, Y
 - · We'll see how to ensure that later
 - Clock signal -- Pulsing signal used to enable latches
 - · Because it ticks like a clock
 - Sequential circuit whose storage components all use clock signals: synchronous circuit
 - Most common type
 - · Asynchronous circuits important topic, but left for advanced course



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Level-sensitive SR latch

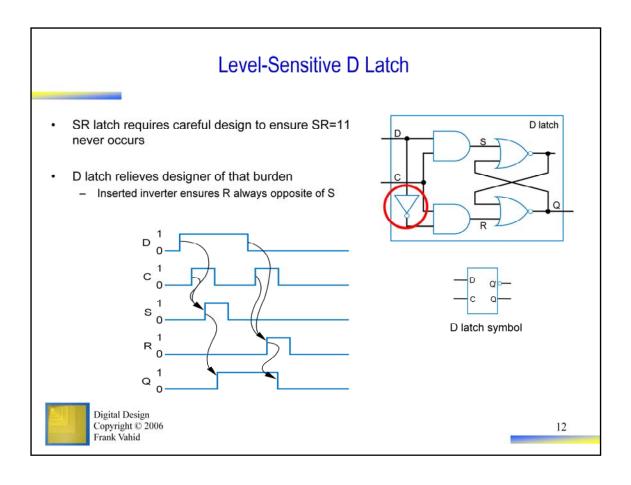
Clocks



- · Clock period: time interval between pulses
 - Above signal: period = 20 ns
- · Clock cycle: one such time interval
 - Above signal shows 3.5 clock cycles
- Clock frequency: 1/period
 - Above signal: frequency = 1 / 20 ns = 50 MHz
 - 1 Hz = 1/s

Period
0.01 ns
0.1 ns
1 ns
10 ns
100 ns



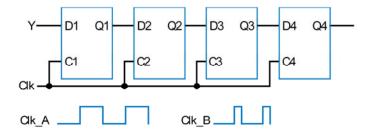


Problem with Level-Sensitive D Latch

- D latch still has problem (as does SR latch)

 When C=1, through how many latches will a signal travel?
- rising edges

- Depends on for how long C=1
 Clk_A -- signal may travel through multiple latches
 - Clk_B -- signal may travel through fewer latches
- Hard to pick C that is just the right length
 - · Can we design bit storage that only stores a value on the rising edge of a clock signal?



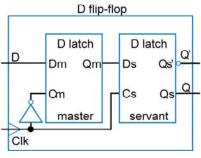


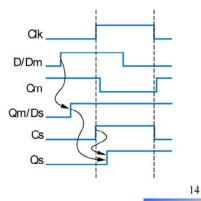
D Flip-Flop

- · Flip-flop: Bit storage that stores on clock edge, not level
- · One design -- master-servant
 - Two latches, output of first goes to input of second, master latch has inverted clock signal
 - So, master loaded when C=0, then servant when C=1
 - When C changes from 0 to 1, master disabled, servant loaded with value that was at D just before C changed -- i.e., value at D during rising edge of C

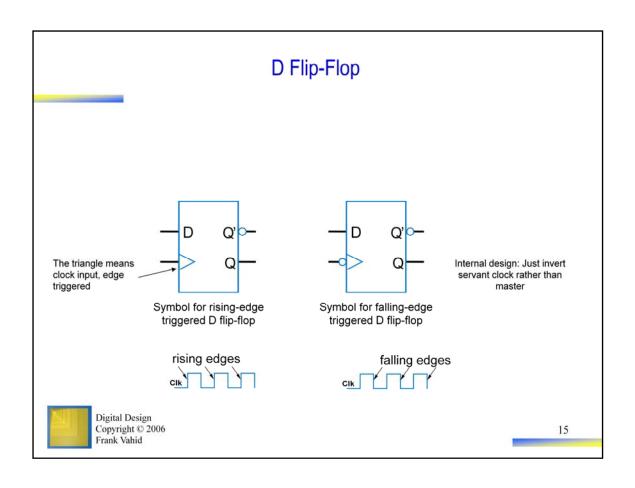


Note: Hundreds of different flipflop designs exist



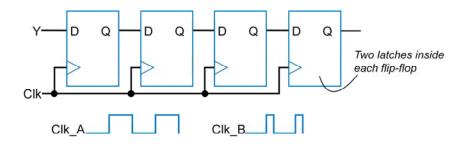






D Flip-Flop

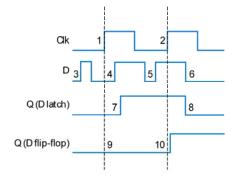
- Solves problem of not knowing through how many latches a signal travels when C=1
 - In figure below, signal travels through exactly one flip-flop, for Clk_A or Clk_B
 - Why? Because on rising edge of Clk, all four flip-flops are loaded simultaneously -- then all four no longer pay attention to their input, until the next rising edge. Doesn't matter how long Clk is 1.



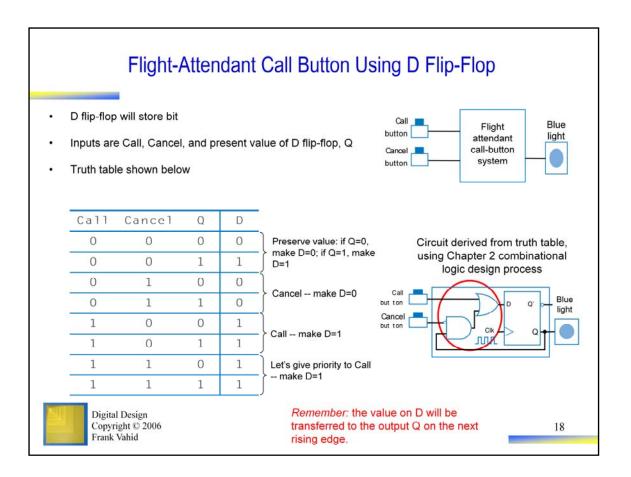


D Latch vs. D Flip-Flop

- · Latch is level-sensitive: Stores D when C=1
- Flip-flop is edge triggered: Stores D when C changes from 0 to 1
 Saying "level-sensitive latch," or "edge-triggered flip-flop," is redundant
 - Two types of flip-flops -- rising or falling edge triggered.
- · Comparing behavior of latch and flip-flop:



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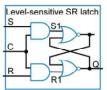


Bit Storage Summary



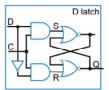
Feature: S=1 sets Q to 1, R=1 resets Q to 0.

Problem: SR=11 yield undefined Q.



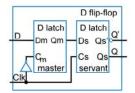
Feature: S and R only have effect when C=1. We can design outside circuit so SR=11 never happens when C=1.

Problem: avoiding SR=11 can be a burden.



Feature: SR can't be 11 if D is stable before and while C=1, and will be 11 for only a brief glitch even if D changes while C=1.

Problem: C=1 too long propagates new values through too many latches: too short may not enable a store.

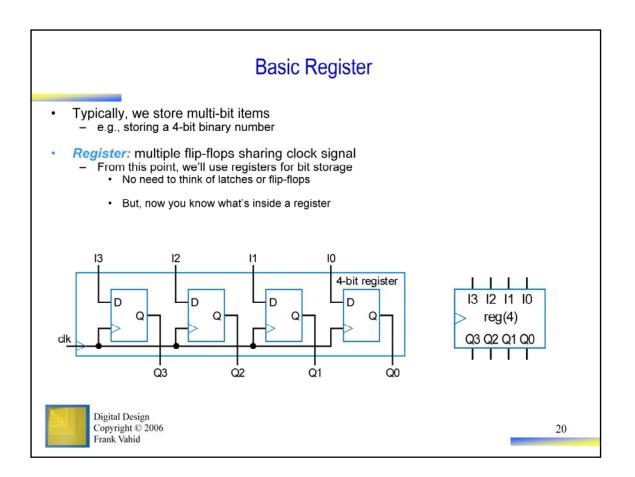


Feature: Only loads D value present at rising clock edge, so values can't propagate to other flip-flops during same clock cycle.

Tradeoff: uses more gates internally than D latch, and requires more external gates than SR – but gate count is less of an issue today.

 We considered increasingly better bit storage until we arrived at the robust D flip-flop bit storage

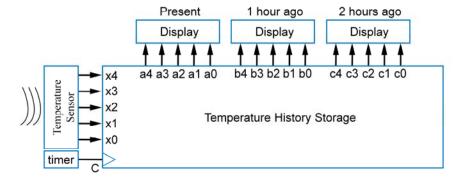




Example Using Registers: Temperature Display

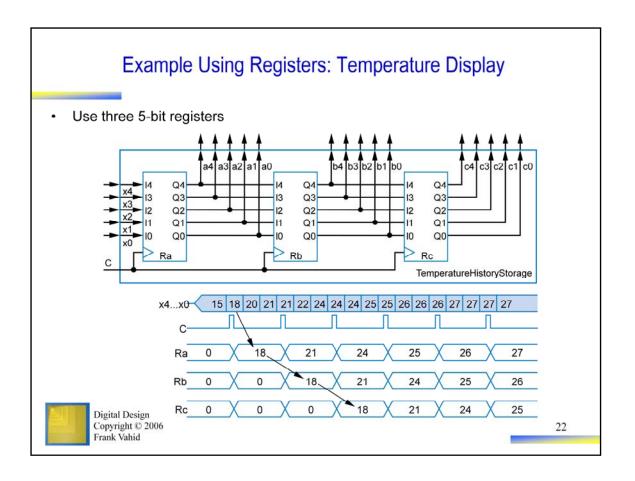
- Temperature history display

 Sensor outputs temperature as 5-bit binary number
 - Timer pulses C every hour
 - Record temperature on each pulse, display last three recorded values



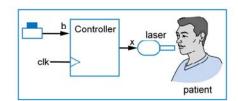


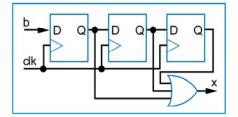
(In practice, we would actually avoid connecting the timer output C to a clock input, instead only connecting an oscillator output to a clock input.)



Finite-State Machines (FSMs) and Controllers

- Want sequential circuit with particular behavior over time
- · Example: Laser timer
 - Push button: x=1 for 3 clock cycles
 - How? Let's try three flip-flops
 - b=1 gets stored in first D flip-flop
 - Then 2nd flip-flop on next cycle, then 3rd flipflop on next
 - OR the three flip-flop outputs, so x should be 1 for three cycles







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3.3

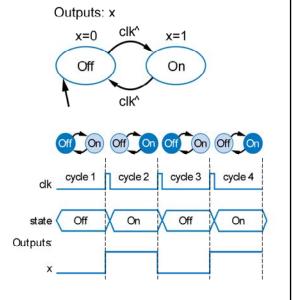
Need a Better Way to Design Sequential Circuits

- Trial and error is not a good design method
 - Will we be able to "guess" a circuit that works for other desired behavior?
 - How about counting up from 1 to 9? Pulsing an output for 1 cycle every 10 cycles? Detecting the sequence 1 3 5 in binary on a 3-bit input?
 - And, a circuit built by guessing may have undesired behavior
 - Laser timer: What if press button again while x=1? x then stays one another 3 cycles. Is that what we want?
- Combinational circuit design process had two important things
 - 1. A formal way to describe desired circuit behavior
 - · Boolean equation, or truth table
 - 2. A well-defined process to convert that behavior to a circuit
- · We need those things for sequence circuit design

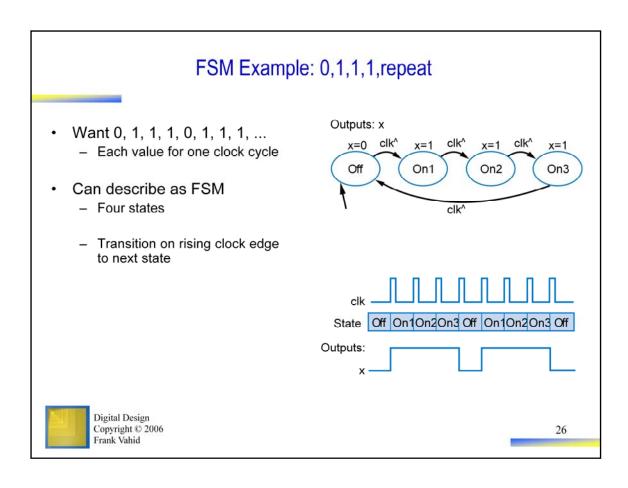


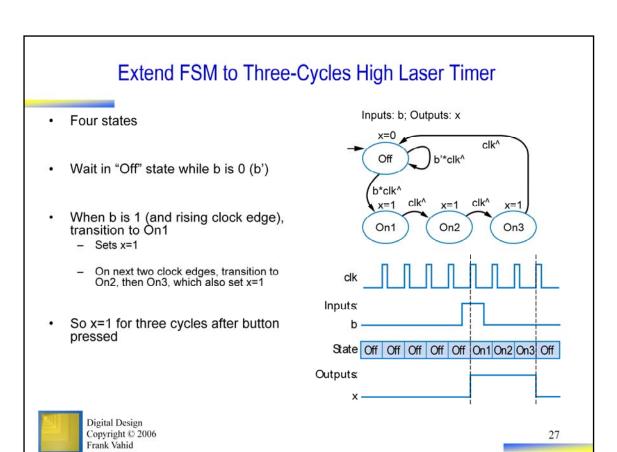
Describing Behavior of Sequential Circuit: FSM

- Finite-State Machine (FSM)
 - A way to describe desired behavior of sequential circuit
 - Akin to Boolean equations for combinational behavior
 - List states, and transitions among states
 - Example: Make x change toggle (0 to 1, or 1 to 0) every clock cycle
 - Two states: "Off" (x=0), and "On" (x=1)
 - Transition from Off to On, or On to Off, on rising clock edge
 - Arrow with no starting state points to initial state (when circuit first starts)



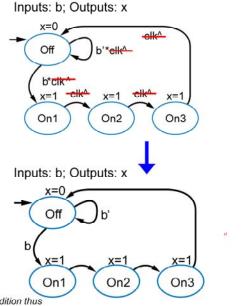






FSM Simplification: Rising Clock Edges Implicit

- Showing rising clock on every transition: cluttered and unnecessary
 - Make implicit -- assume every edge has rising clock, even if not shown.
 - Eg., it is understood that a transition out of a state is on a clock edge.
 - What if we wanted a transition without a rising edge
 - We don't consider such asynchronous FSMs -- less common, and advanced topic
 - Only consider synchronous FSMs -rising edge on every transition

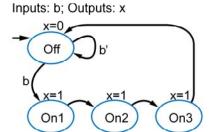




Note: Transition with no associated condition thus transistions to next state on next clock cycle

FSM Definition

- FSM consists of
 - Set of states
 - Ex: {Off, On1, On2, On3}
 - Set of inputs, set of outputs
 - Ex: Inputs: {x}, Outputs: {b}
 - Initial state
 - Ex: "Off"
 - Set of transitions
 - · Describes next states
 - · Eg: Has 5 transitions
 - Set of actions
 - · Sets outputs while in states
 - Eg: x=0, x=1, x=1, and x=1



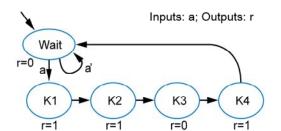
We often draw FSM graphically, known as **state diagram**

Can also use table (state table), or textual languages



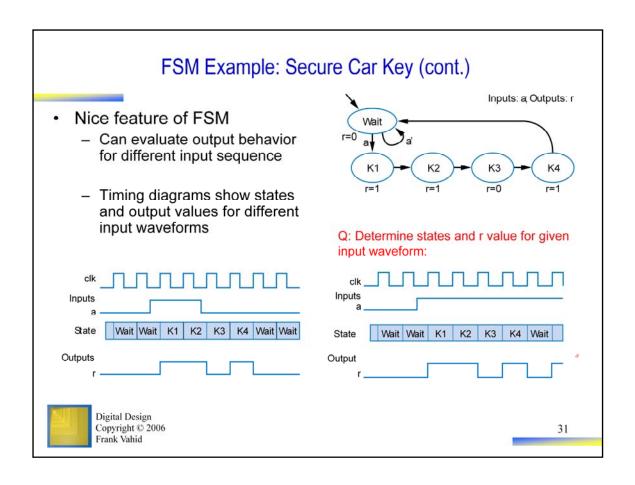
FSM Example: Secure Car Key

- Many new car keys include tiny computer chip
 - When car starts, car's computer (under engine hood) requests identifier from key
 - Key transmits identifier
 - · If not, computer shuts off car
- FSM
 - Wait until computer requests ID (a=1)
 - Transmit ID (in this case, 1101)



a.k.a., A Sequencer



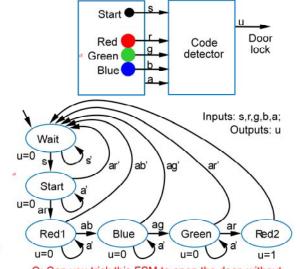


FSM Example: Code Detector

- Unlock door (u=1) only when buttons pressed in sequence:
 - start, then red, blue, green, red
- Input from each button: s, r, g, b

 Also, output a indicates that some colored button pressed
- **FSM**
 - Wait for start (s=1) in "Wait"
 - Once started ("Start")
 - · If see red, go to "Red1"
 - · Then, if see blue, go to "Blue"
 - · Then, if see green, go to "Green"
 - Then, if see red, go to "Red2"

 In that state, open the door (u=1)
 - Wrong button at any step, return to "Wait", without opening door

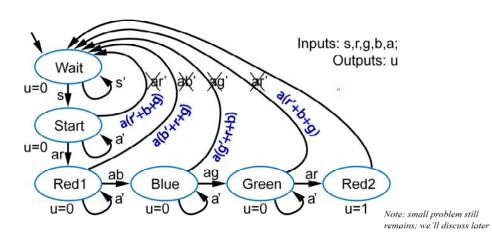


Q: Can you trick this FSM to open the door, without knowing the code?

A: Yes, hold all buttons simultaneously

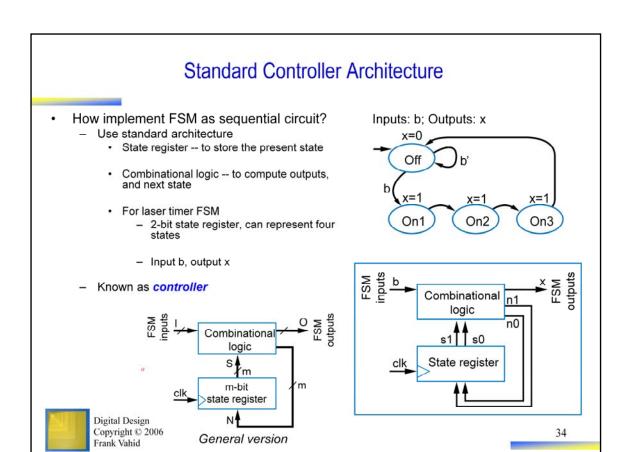
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Improve FSM for Code Detector



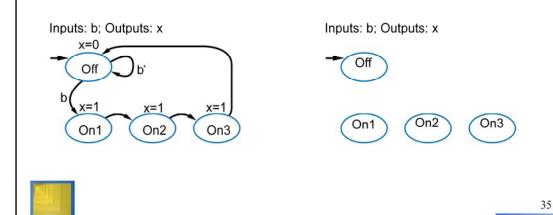
- New transition conditions detect if wrong button pressed, returns to "Wait"
- · FSM provides formal, concrete means to accurately define desired behavior





State Diagram Example

Modify the laser pulse generator state diagram (below left), so that the new FSM will only produce one pulse (3 clk cycles wide) for each actuation of 'b' ... or stated another way, one pulse out for one pulse in.



3.4

Controller Design

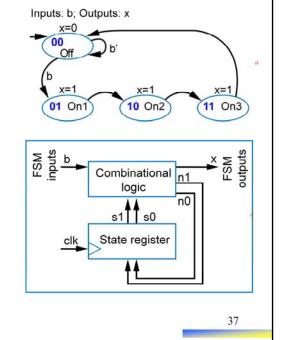
• Five step controller design process

	Step	Description
Step 1	Capture the FSM	Create an FSM that describes the desired behavior of the controller.
Step 2	Create the architecture	Create the standard architecture by using a state register of appropriate width, and combinational logic with inputs being the state register bits and the FSM inputs and outputs being the next state bits and the FSM outputs.
Step 3	Encode the states	Assign a unique binary number to each state. Each binary number representing a state is known as an <i>encoding</i> . Any encoding will do as long as each state has a unique encoding.
Step 4	Create the state table	Create a truth table for the combinational logic such that the logic will generate the correct FSM outputs and next state signals. Ordering the inputs with state bits first makes this truth table describe the state behavior, so the table is a state table.
Step 5	Implement the combinational logic	Implement the combinational logic using any method.

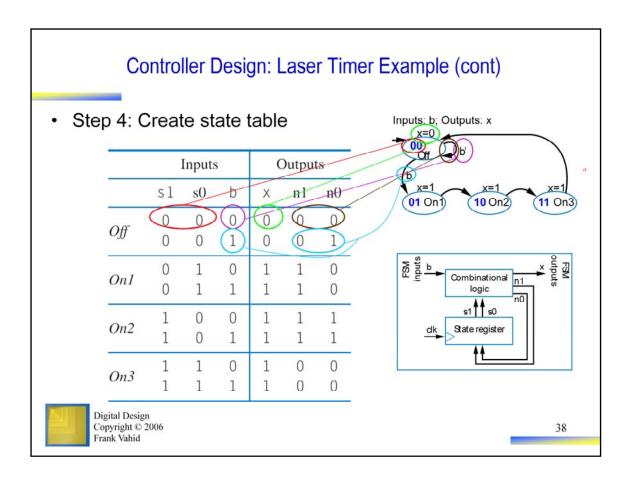


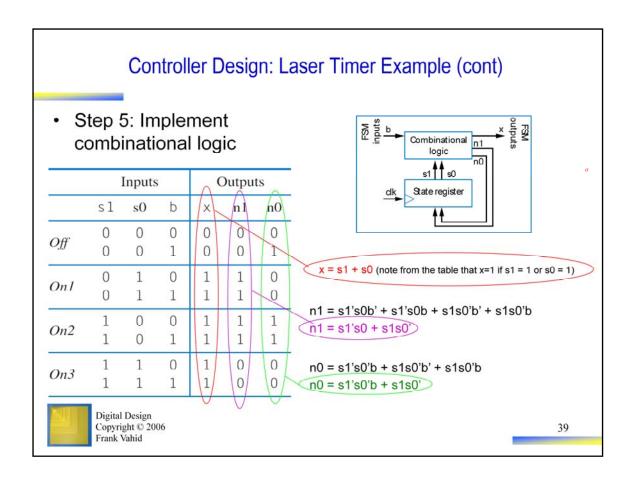


- Step 1: Capture the FSM
 - Already done
- Step 2: Create architecture
 - 2-bit state register (for 4 states)
 - Input b, output x
 - Next state signals n1, n0
- Step 3: Encode the states
 - Any encoding with each state unique will work (in blue)





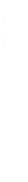


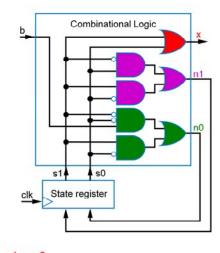


Controller Design: Laser Timer Example (cont)

 Step 5: Implement combinational logic (cont)

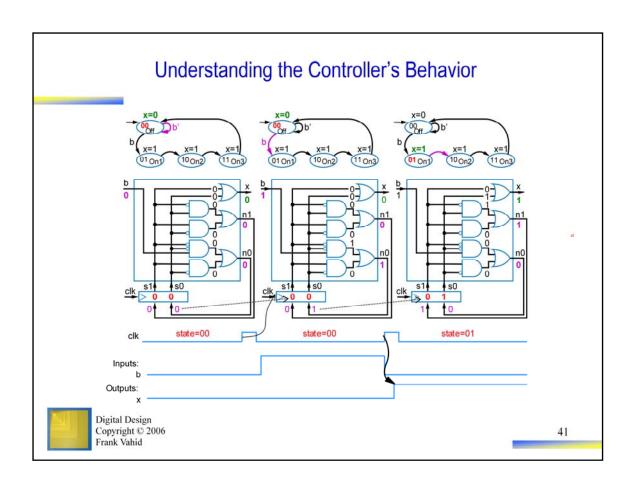
	Inputs			Outputs		
	s1	s0	b	Х	n1	n0
Off	0	0	0	0	0	0
	0	0	1	0	0	1
On1	0	1	0	1	1	0
	0	1	1	1	1	0
On2	1	0	0	1	1	1
	1	0	1	1	1	1
On3	1	1	0	1	0	0
	1	1	1	1	0	0



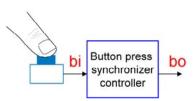


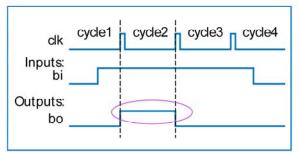
x = s1 + s0 n1 = s1's0 + s1s0'n0 = s1's0'b + s1s0'

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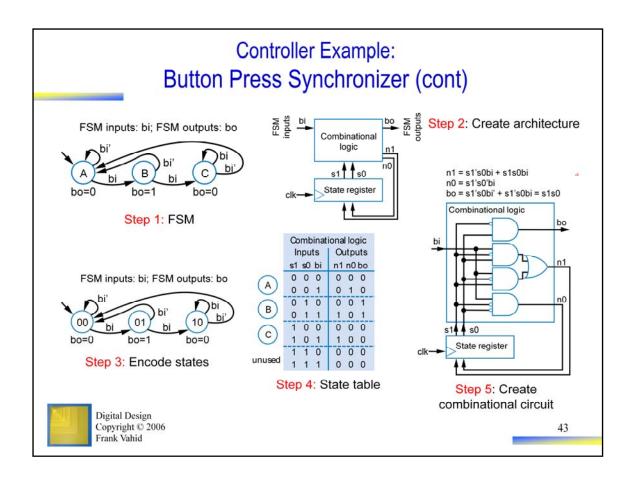


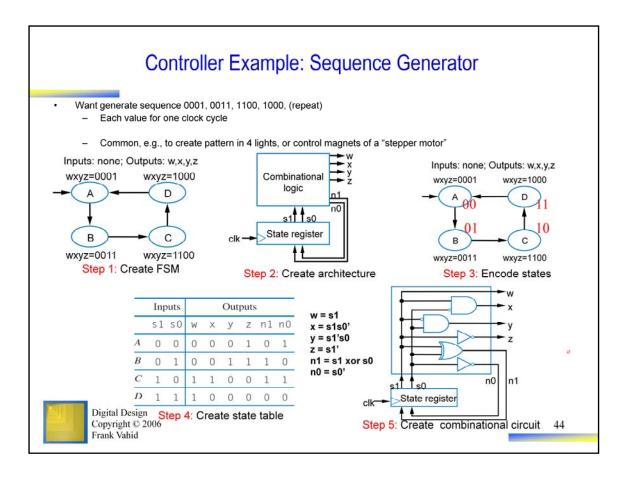


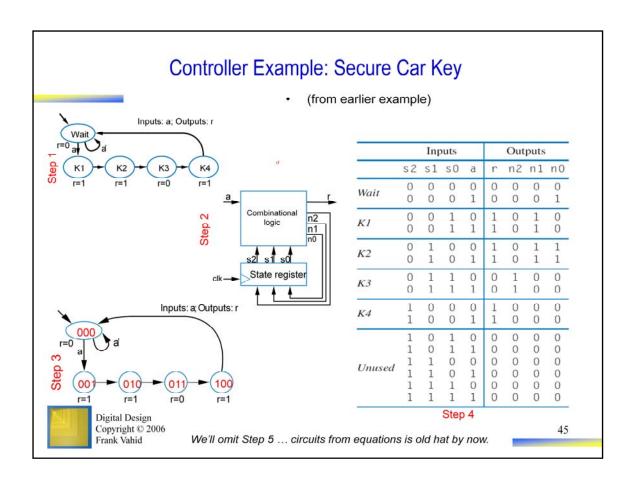


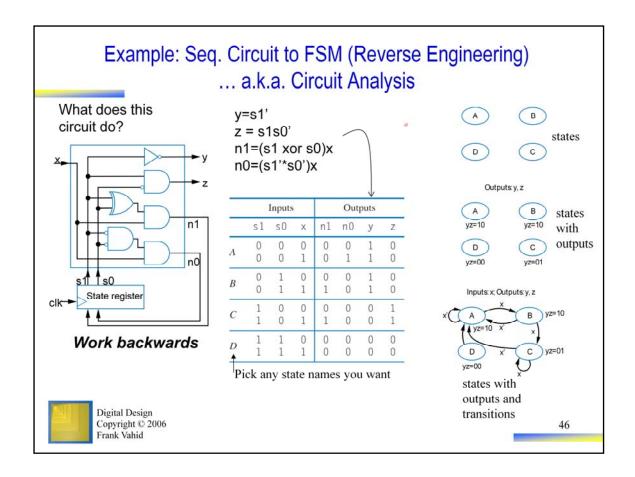
- Want simple sequential circuit that converts button press to single cycle duration, regardless of length of time that button actually pressed
 - We assumed such an ideal button press signal in earlier example, like the button in the laser timer controller

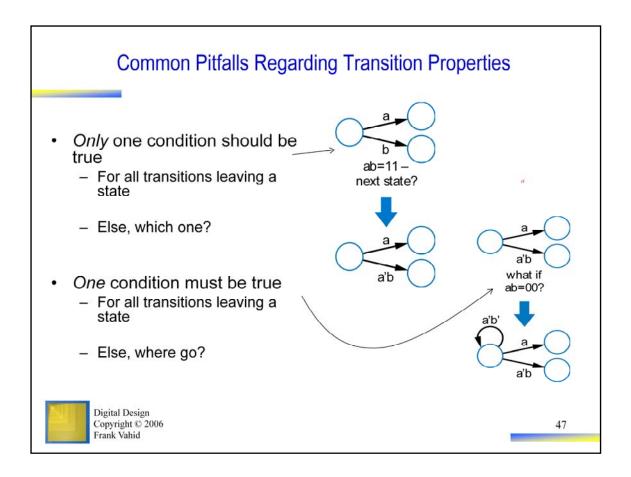






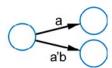






Verifying Correct Transition Properties

- · Can verify using Boolean algebra
 - Only one condition true: AND of each condition pair (for transitions leaving a state) should equal 0 → proves pair can never simultaneously be true
 - One condition true: OR of all conditions of transitions leaving a state) should equal 1 → proves at least one condition must be true
 - Example



Answer:

```
a * a'b
= (a * a') * b
= 0 * b
= 0
OK!
```

a + a'b = a*(1+b) + a'b = a + ab + a'b = a + (a+a')b = a + b Fails! Might not be 1 (i.e., a=0, b=0)

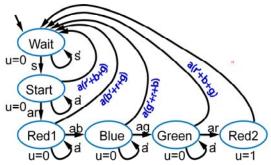
Q: For shown transitions, prove whether:

- * Only one condition true (AND of each pair is always 0)
- * One condition true (OR of all transitions is always 1)



Evidence that Pitfall is Common

- Recall code detector FSM
 - We "fixed" a problem with the transition conditions
 - Do the transitions obey the two required transition properties?
 - Consider transitions of state Start, and the "only one true" property



$$ar * a' a' a(r'+b+g)$$
 $ar * a(r'+b+g)$ $= (a*a')r = 0*r = (a*a)*(r'+b+g) = 0*(r'+b+g)$ $= (a*a)*r*(r'+b+g) = a*r*(r'+b+g)$ $= 0 = 0 = 0 = arr'+arb+arg$ $= 0 + arb+arg$ $= arb + arg$ $= ar(b+g)$ A: ar

Fails! Means that two of Start's transitions could be true

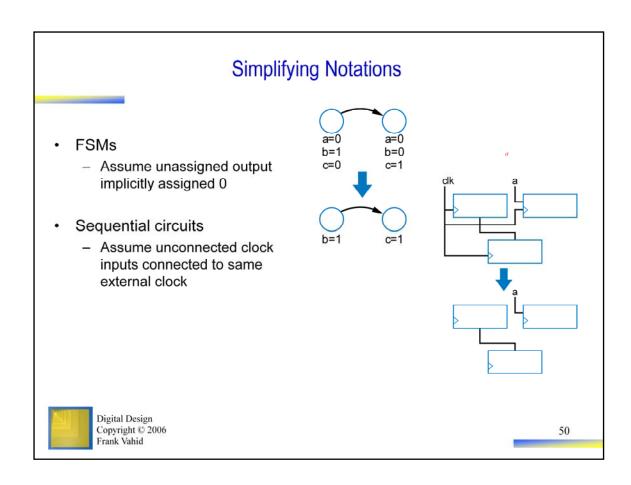
Intuitively. press red and blue buttons at same time: conditions ar, and a(r'+b+g) will both be true. Which one should be taken?

Q: How to solve?

A: ar should be arb'g' (likewise for ab, ag, ar)

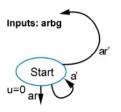
Note: As evidence the pitfall is common, we admit the mistake was not intentional. A reviewer of the book caught it.



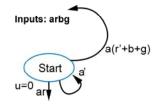


Solving this pitfall ... a different point of view

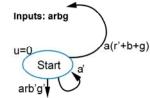
- · The rules mentioned by the textbook author can be simplified to one statement ...
 - "There must be one and only one path leaving a state for each input combination (that's inputs & current state)"
- Best way to check the paths is to find the minterms for each path ... each minterm should be present
 once and only once for all paths leaving the state ... think about how to do the state transition table.



No problem with transitions here ... problem with FSM operation per spec



Appears to solve spec problem ... however, there are more than one path out of 'Start' for inputs m13, m14 and m15



Best solution makes sense ... a AND r but NOT b AND NOT g move the FSM forward.

Defining the FSM using VHDL

- Using the model put forth by the author ... there will be two process statements
 - Combinational logic (next state logic and output logic combined)
 - State register
- · Modeling the state register
 - Assume cs (current state) and ns (next state) are bit vectors

```
process (clk)
begin
  if (clk'event and clk='1') then
    cs <= ns;
  end if;
end process;</pre>
```

This register is built with rising edge triggered D-FF's.



FSM w/ VHDL (cont.)

 For a falling-edge triggered register ...

```
process (clk)
begin
  if (clk'event and
  clk='0') then
      cs <= ns;
  end if;
end process;</pre>
```

 For a rising-edge triggered register, with async. reset ...

```
process (clk, reset)
begin
if (reset = 'l') then
  cs <= "000";
elsif (clk'event and clk='l') then
  cs <= ns;
  end if;
end process;</pre>
```

 For a falling-edge triggered register, with sync. active-low reset ...

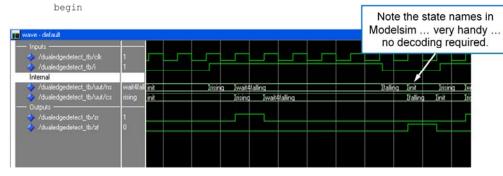
```
process (clk, reset)
begin
  if (clk'event and clk='0') then
    if (reset = '0') then
      cs <= "000";
    else
      cs <= ns;
    end if;
end if;</pre>
```

end if; end if; end process;

FSM w/ VHDL (cont.)

- · If you define enumerate a new type, life will be easier
 - Example:

```
architecture Behavioral of dualEdgeDetect is
  type stateType is (init, rising, wait4falling, falling);
  signal ns, cs: stateType;
```



 Another benefit for using enumerated types for naming states is when designing the combinatorial logic block



FSM w/ VHDL (cont.)

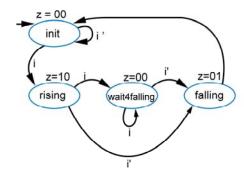
process(i, cs)

case cs is

begin

 Setup combinatorial logic block in a process statement and a case statement:

Inputs: i; Outputs: z = zr,zf



```
when init =>
         if i='0' then ns <= init;
         else
                        ns <= rising;
          end if;
          zr <= '0';
                         zf <= '0';
      when rising =>
         if i='0' then ns <=falling;
                        ns <= wait4falling;
          else
          end if;
         zr <= '1'; zf <= '0';
       when wait4falling =>
         if i='0' then ns <= falling;
                       ns <= wait4falling;
          else
          end if;
         zr <= '0';
                         zf <= '0';
       when falling =>
         ns <= init;
          zr <= '0';
                         zf <= '1';
       when others =>
         ns <= init;
         zr <= '0';
                        zf <= '0';
     end case;
end process;
```

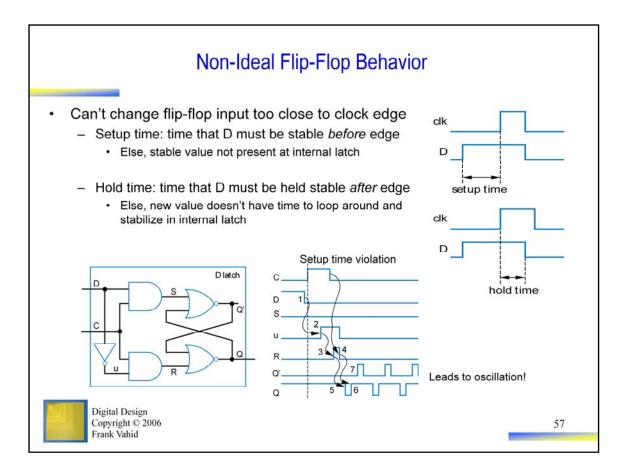


3.5

More on Flip-Flops and Controllers

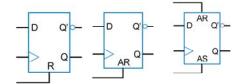
- · Other flip-flop types
 - SR flip-flop: like SR latch, but edge triggered
 - JK flip-flop: like SR (S→J, R→K)
 - But when JK=11, toggles
 - 1→0, 0→1
 - T flip-flop: JK with inputs tied together
 - · Toggles on every rising clock edge
 - Previously utilized to minimize logic outside flip-flop
 - · Today, minimizing logic to such extent is not as important
 - · D flip-flops are thus by far the most common

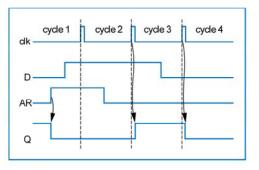




Flip-Flop Set and Reset Inputs

- Some flip-flops have additional inputs
 - Synchronous reset: clears Q to 0 on next clock edge
 - Synchronous set: sets Q to 1 on next clock edge
 - Asynchronous reset: clear Q to 0 immediately (not dependent on clock edge)
 - · Example timing diagram shown
 - Asynchronous set: set Q to 1 immediately



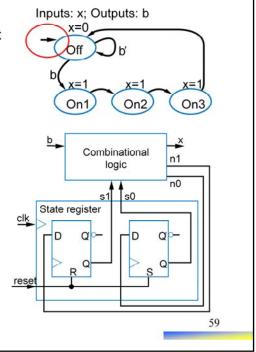




Initial State of a Controller

- All our FSMs had initial state
 - But our sequential circuit designs did not
 - Can accomplish using flip-flops with reset/set inputs
 - · Shown circuit initializes flip-flops to 01
 - Designer must ensure reset input is 1 during power up of circuit
 - · By electronic circuit design
 - Most common method is to encode the initial state with all zeros and connect the resets of the D-FF's to the clear or reset input.





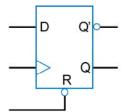
Glitching

- Glitch: Temporary values on outputs that appear soon after input changes, before stable new output values
- Designer must determine whether glitching outputs may pose a problem
 - If so, may consider adding flip-flops to outputs
 - Delays output by one clock cycle, but may be OK
 - · Referred to as "pipelining the outputs".



Active Low Inputs

- We've assumed input action occur when input is 1
 - Some inputs are instead active when input is 0 -- "active low"
 - Shown with inversion bubble
 - So to reset the shown flip-flop, set R=0. Else, keep R=1.





Chapter Summary

- · Sequential circuits
 - Have state
- Created robust bit-storage device: D flip-flop
 - Put several together to build register, which we used to hold state
- · Defined FSM formal model to describe sequential behavior
 - Using solid mathematical models -- Boolean equations for combinational circuit, and FSMs for sequential circuits -- is very important.
- Defined 5-step process to convert FSM to sequential circuit
 - Controller
- So now we know how to build the class of sequential circuits known as controllers

