

Digital Design

Chapter 1: Introduction

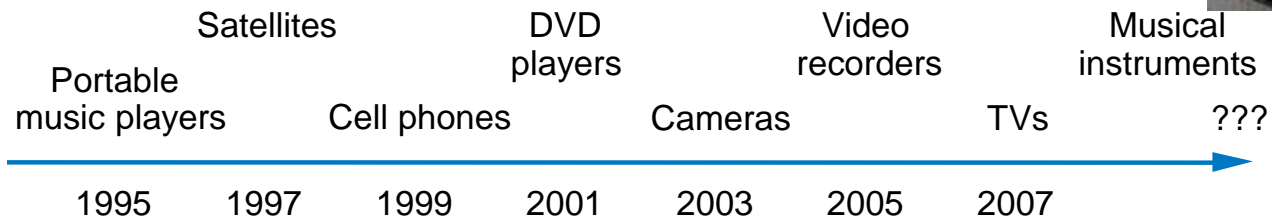
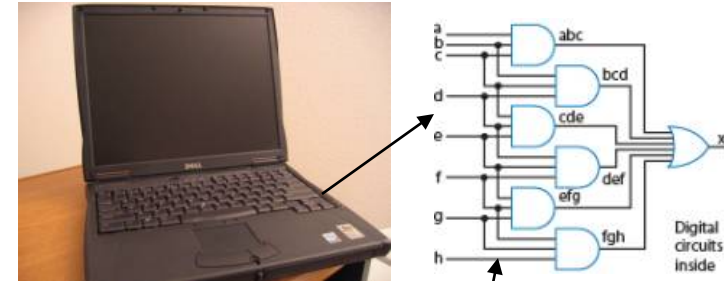
Slides to accompany the textbook *Digital Design, with RTL Design, VHDL, and Verilog*, 2nd Edition,
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Why Study Digital Design?

- Look “under the hood” of computers
 - Solid understanding --> confidence, insight, even better programmer when aware of hardware resource issues
- Electronic devices becoming digital
 - Enabled by shrinking and more capable chips
 - Enables:
 - Better devices: Sound recorders, cameras, cars, cell phones, medical devices,...
 - New devices: Video games, PDAs, ...
 - Known as “embedded systems”
 - Thousands of new devices every year
 - Designers needed: Potential career direction



- Years shown above indicate when digital version began to *dominate*
 - (Not the first year that a digital version appeared)

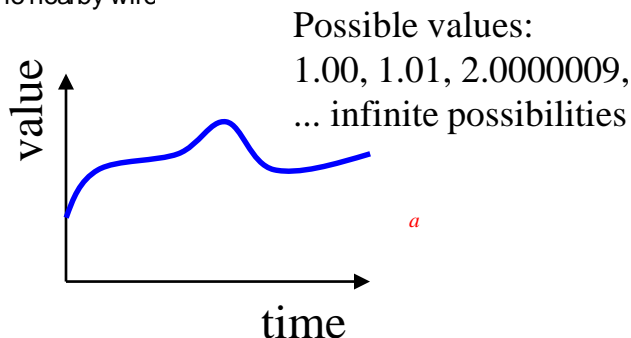
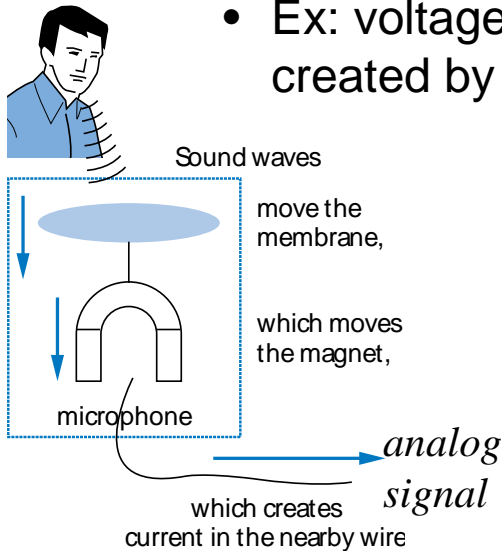


What Does "Digital" Mean?

- Analog signal

- Infinite possible values

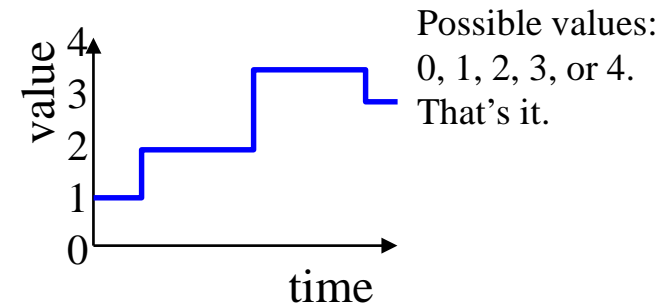
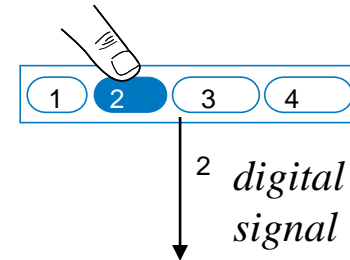
- Ex: voltage on a wire created by microphone



- Digital signal

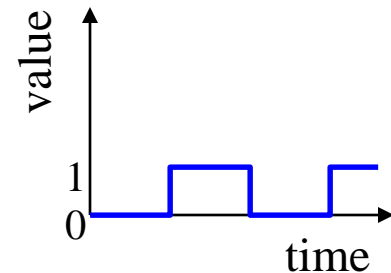
- Finite possible values

- Ex: button pressed on a keypad



Digital Signals with Only Two Values: Binary

- **Binary** digital signal -- only *two* possible values
 - Typically represented as **0** and **1**
 - One *binary digit* is a **bit**
 - We'll only consider *binary* digital signals
 - Binary is popular because
 - Transistors, the basic digital electric component, operate using *two* voltages (more in Chpt. 2)
 - Storing/transmitting one of *two* values is easier than three or more (e.g., loud beep or quiet beep, reflection or no reflection)



Example of Digitization Benefit

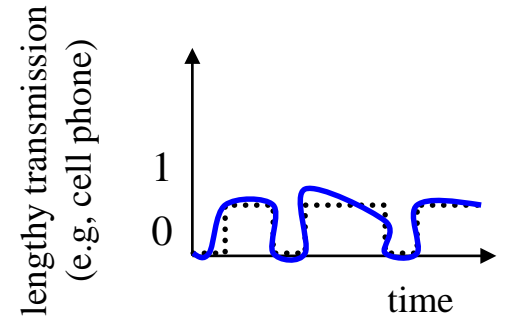
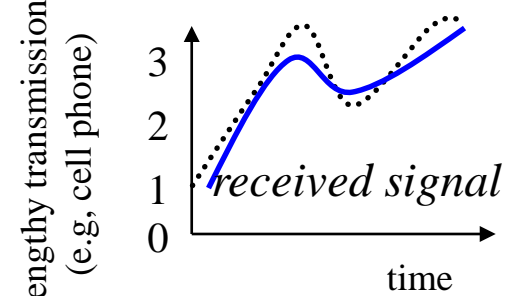
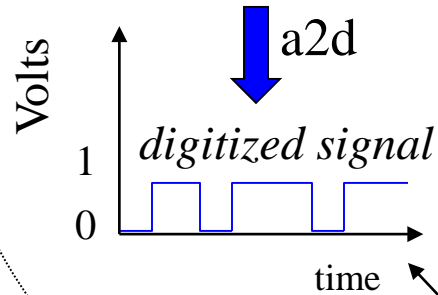
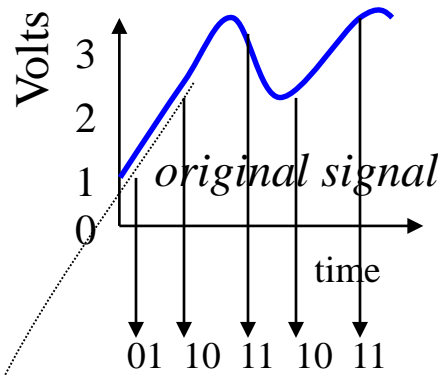
- Analog signal (e.g., audio, video) may lose quality
 - Voltage levels not saved/copied/transmitted perfectly
- Digitized version enables near-perfect save/cpy/tran.
 - “Sample” voltage at particular rate, save sample using bit encoding
 - Voltage levels still not kept perfectly
 - But we can distinguish 0s from 1s

Let bit encoding be:

1 V: “01”

2 V: “10”

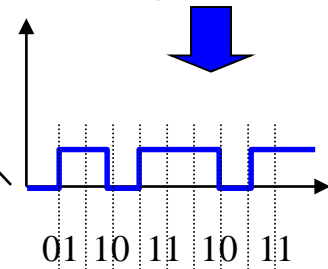
3 V: “11”



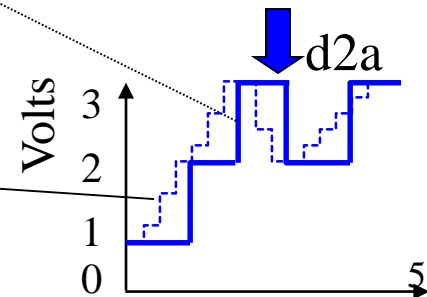
Not a perfect re-creation due to a2d and d2a

same

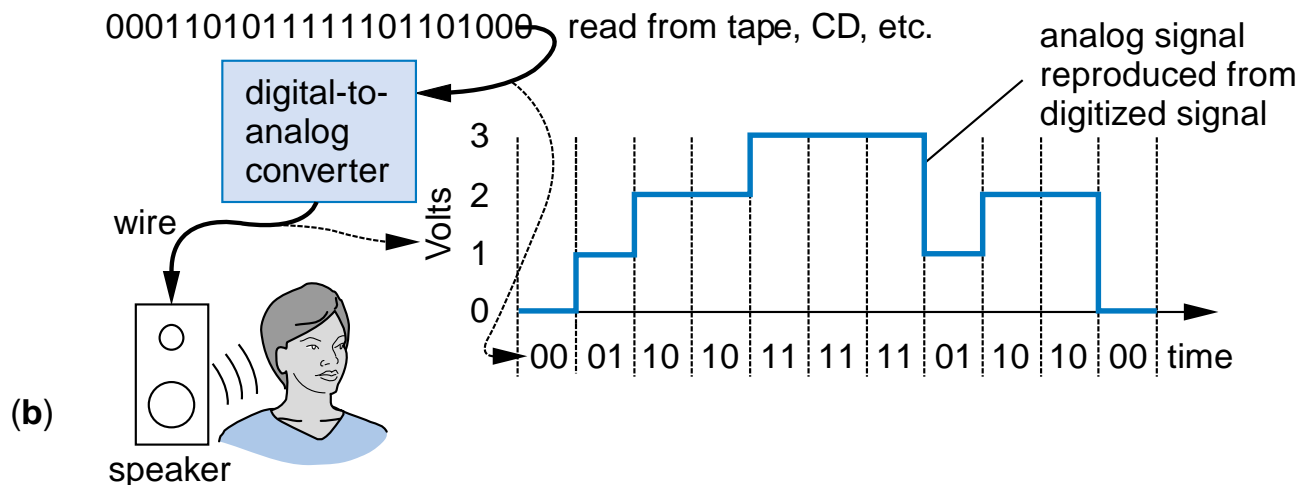
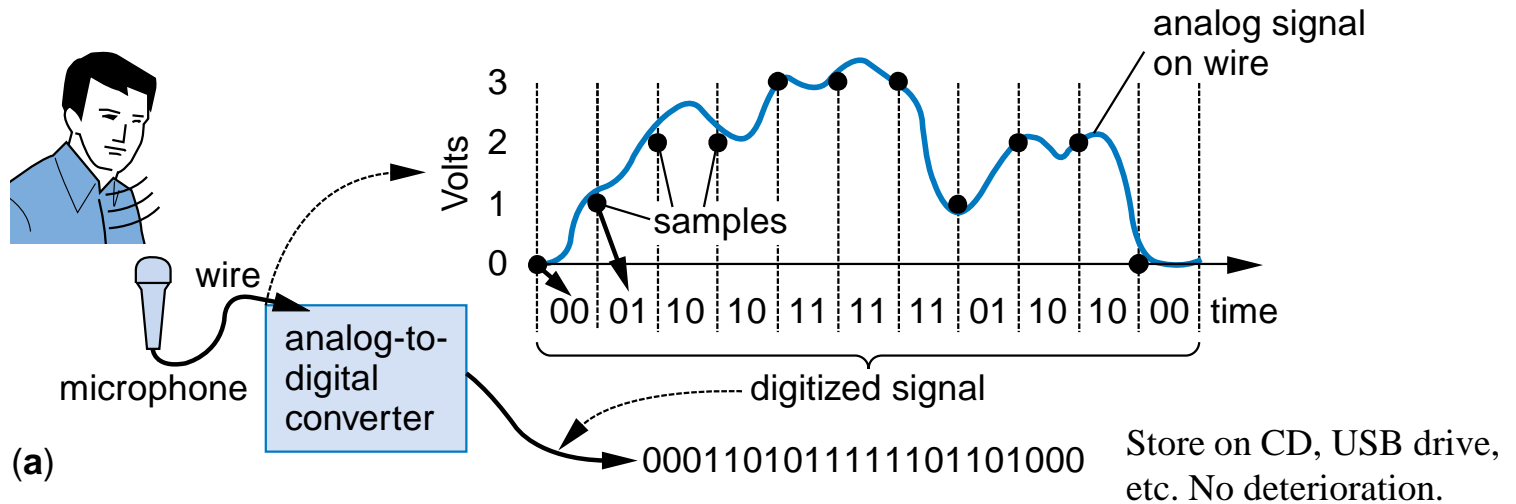
Can fix—distinguish 0s/1s, restore



Higher sampling rate and more bits per encoding improves re-creation



Digitization Benefit: Can Store on Digital Media



Digitized Audio: Compression Benefit

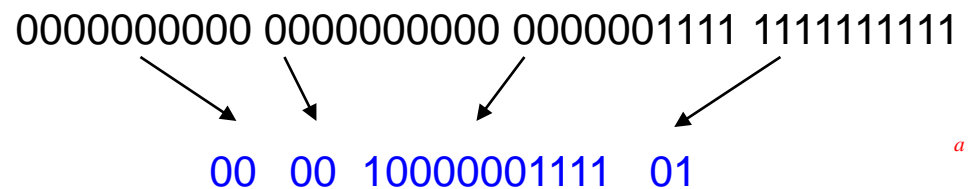
- Digitized audio can be compressed
 - e.g., MP3s
 - A CD can hold about 20 songs uncompressed, but about 200 compressed
- Compression also done on digitized pictures (jpeg), movies (mpeg), and more
- Digitization has many other benefits too

Example compression scheme:

00 means 0000000000

01 means 1111111111

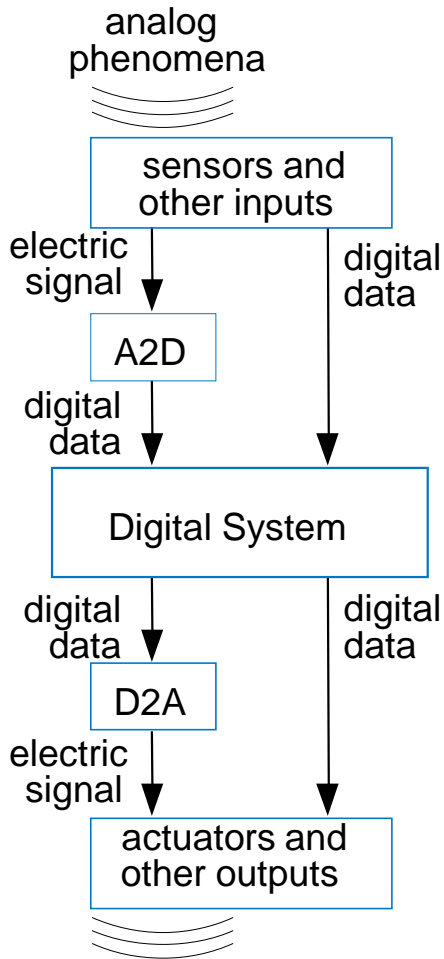
1X means X



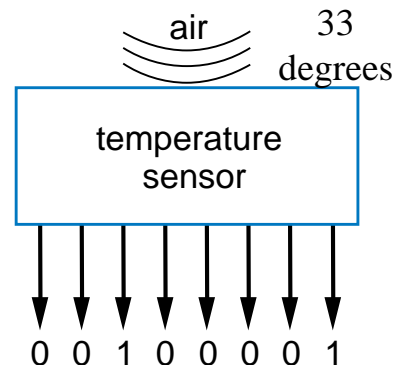
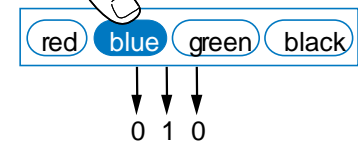
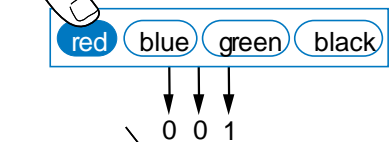
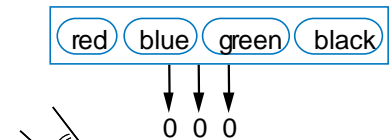
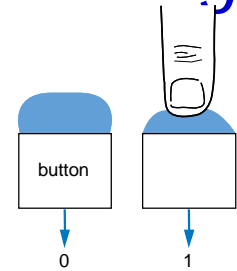
a



How Do We Encode Data as Binary for Our Digital System?



- Some inputs inherently binary
 - Button: not pressed (0), pressed (1)
- Some inputs inherently digital
 - Just need encoding in binary
 - e.g., multi-button input: encode red=001, blue=010, ...
- Some inputs analog
 - Need analog-to-digital conversion
 - As done in earlier slide -- sample and encode with bits



How to Encode Text: ASCII, Unicode

- ASCII: 7- (or 8-) bit encoding of each letter, number, or symbol
- Unicode: Increasingly popular 16-bit encoding
 - Encodes characters from various world languages

Sample ASCII encodings

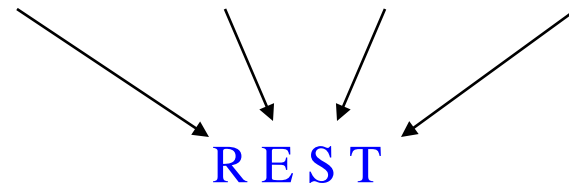
Encoding	Symbol
010 0000	<space>
010 0001	!
010 0010	"
010 0011	#
010 0100	\$
010 0101	%
010 0110	&
010 0111	'
010 1000	(
010 1001)
010 1010	*
010 1011	+
010 1100	,
010 1101	-
010 1110	.
010 1111	/

Encoding	Symbol	Encoding	Symbol
100 0001	A	100 1110	N
100 0010	B	100 1111	O
100 0011	C	101 0000	P
100 0100	D	101 0001	Q
100 0101	E	101 0010	R
100 0110	F	101 0011	S
100 0111	G	101 0100	T
100 1000	H	101 0101	U
100 1001	I	101 0110	V
100 1010	J	101 0111	W
100 1011	K	101 1000	X
100 1100	L	101 1001	Y
100 1101	M	101 1010	Z

Encoding	Symbol
110 0001	a
110 0010	b
...	
111 1001	y
111 1010	z
011 0000	0
011 0001	1
011 0010	2
011 0011	3
011 0100	4
011 0101	5
011 0110	6
011 0111	7
011 1000	8
011 1001	9

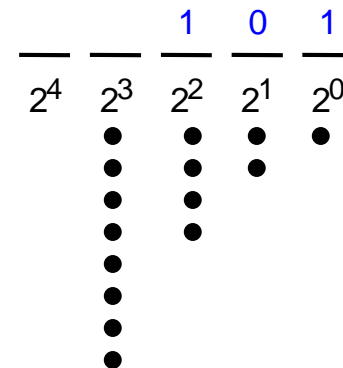
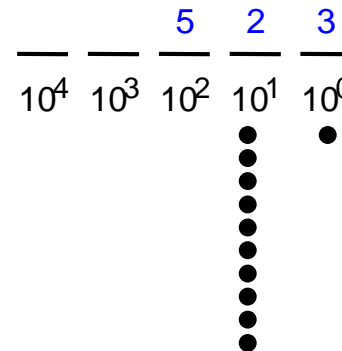
Question:
What does this ASCII bit sequence represent?

1010010 1000101 1010011 1010100

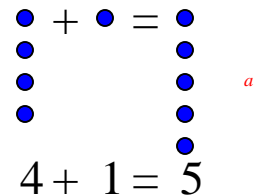


How to Encode Numbers: Binary Numbers

- Each position represents a quantity; symbol in position means how many of that quantity
 - Base ten (*decimal*)
 - Ten symbols: 0, 1, 2, ..., 8, and 9
 - More than 9 -- next position
 - So each position power of 10
 - Nothing special about base 10 -- used because we have 10 fingers
 - Base two (*binary*)
 - Two symbols: 0 and 1
 - More than 1 -- next position
 - So each position power of 2

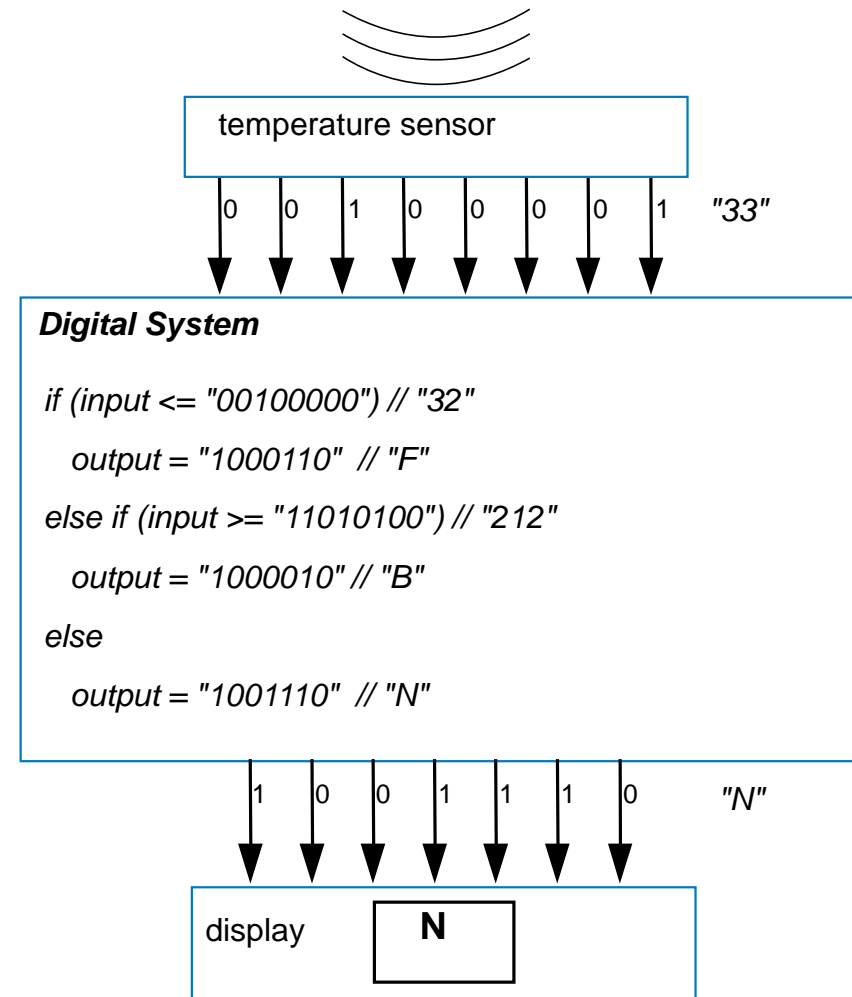


Q: How much?



Using Digital Data in a Digital System

- A temperature sensor outputs temperature in binary
- The system reads the temperature, outputs ASCII code:
 - “F” for freezing (0-32)
 - “B” for boiling (212 or more)
 - “N” for normal
- A display converts its ASCII input to the corresponding letter



Converting from Binary to Decimal

- Just add weights
 - 1_2 is just $1 \cdot 2^0$, or 1_{10} .
 - 110_2 is $1 \cdot 2^2 + 1 \cdot 2^1 + 0 \cdot 2^0$, or 6_{10} . We might think of this using base ten weights: $1 \cdot 4 + 1 \cdot 2 + 0 \cdot 1$, or 6.
 - 10000_2 is $1 \cdot 16 + 0 \cdot 8 + 0 \cdot 4 + 0 \cdot 2 + 0 \cdot 1$, or 16_{10} .
 - 10000111_2 is $1 \cdot 128 + 1 \cdot 4 + 1 \cdot 2 + 1 \cdot 1 = 135_{10}$. Notice this time that we didn't bother to write the weights having a 0 bit.
 - 00110_2 is the same as 110_2 above — the leading 0's don't change the value.

Useful to know powers of 2:

—	—	—	—	—	—	—	—	—	—
2^9	2^8	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
—	—	—	—	—	—	—	—	—	—
512	256	128	64	32	16	8	4	2	1

Practice counting up by powers of 2:

512 256 128 64 32 16 8 4 2 1



Converting from Decimal to Binary

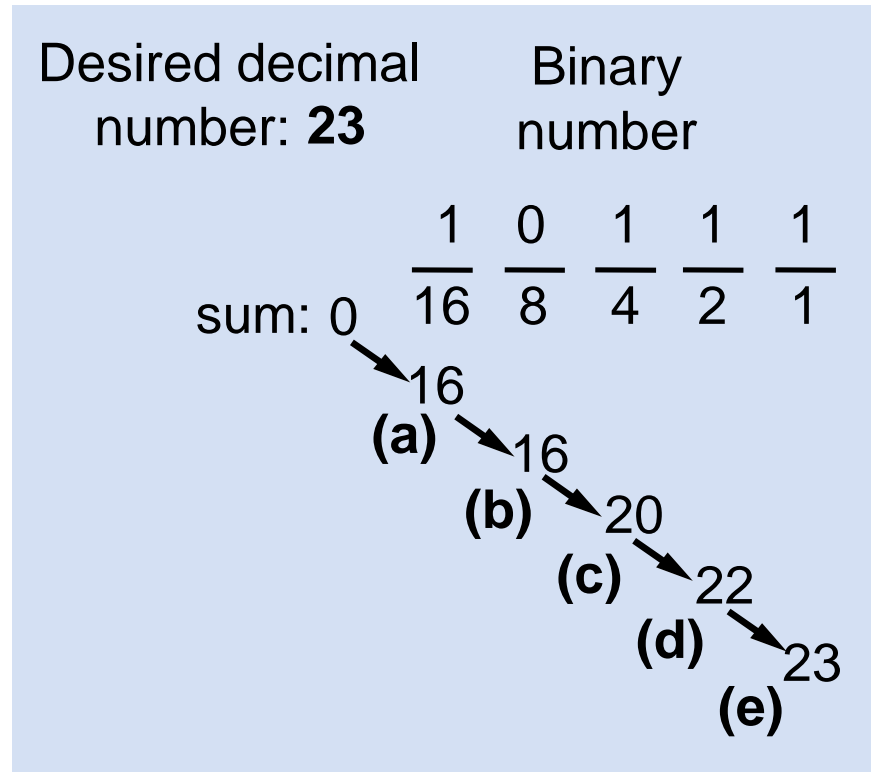
- Put 1 in leftmost place without sum exceeding number
- Track sum

	Desired decimal number: 12	Current sum	Binary number
(a)	16 > 12, too big; Put 0 in 16's place	0	$\frac{0}{16}$ $\frac{\quad}{8}$ $\frac{\quad}{4}$ $\frac{\quad}{2}$ $\frac{\quad}{1}$
(b)	8 ≤ 12, so put 1 in 8's place, current sum is 8	8	$\frac{0}{16}$ $\frac{1}{8}$ $\frac{\quad}{4}$ $\frac{\quad}{2}$ $\frac{\quad}{1}$
(c)	8+4=12 ≤ 12, so put 1 in 4's place, current sum is 12	12	$\frac{0}{16}$ $\frac{1}{8}$ $\frac{1}{4}$ $\frac{\quad}{2}$ $\frac{\quad}{1}$
(d)	Reached desired 12, so put 0s in remaining places	<i>done</i>	$\frac{0}{16}$ $\frac{1}{8}$ $\frac{1}{4}$ $\frac{0}{2}$ $\frac{0}{1}$



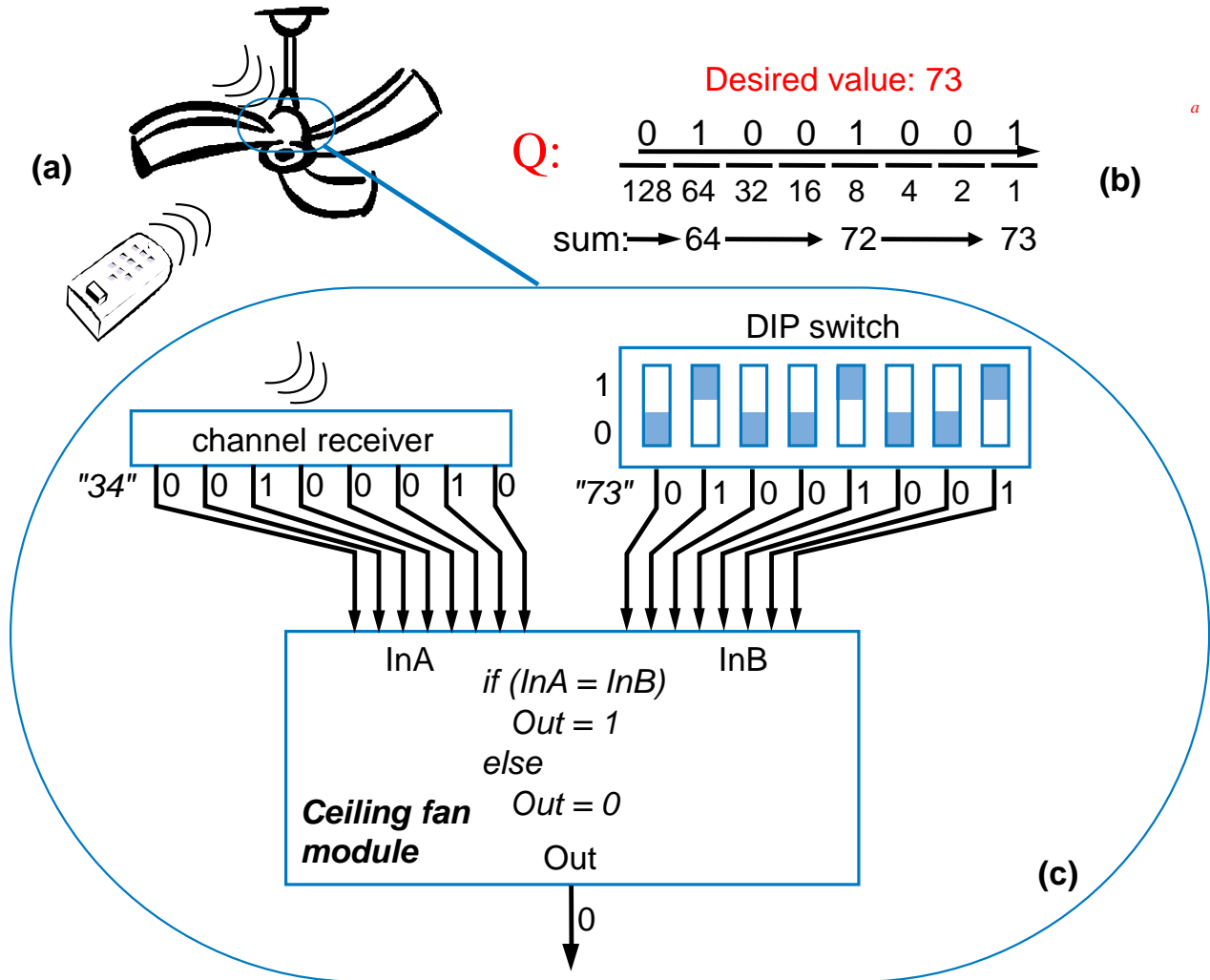
Converting from Decimal to Binary

- Example using a more compact notation

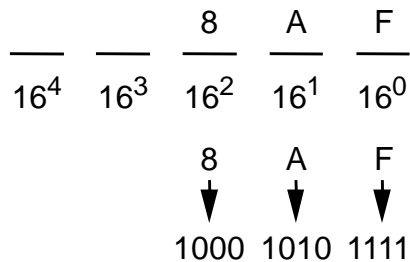


Example: DIP-Switch Controlled Channel

- Ceiling fan receiver should be set in factory to respond to channel "73"
- Convert 73 to binary, set DIP switch accordingly



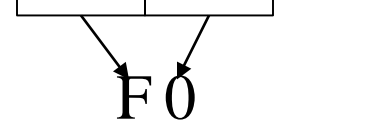
Base Sixteen: Another Base Used by Designers



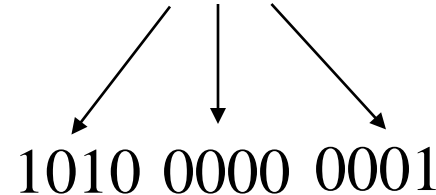
- Nice because each position represents four base-two positions
 - Compact way to write binary numbers
- Known as *hexadecimal*, or just *hex*

hex	binary	hex	binary
0	0000	8	1000
1	0001	9	1001
2	0010	A	1010
3	0011	B	1011
4	0100	C	1100
5	0101	D	1101
6	0110	E	1110
7	0111	F	1111

Q: Write **11110000** in hex



Q: Convert hex **A01** to binary

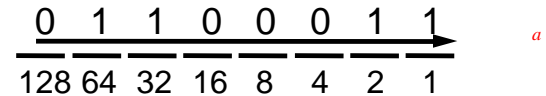


Decimal to Hex

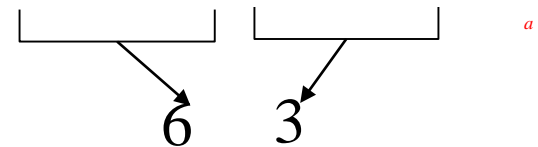
- Easy method: convert to binary first, then binary to hex

Convert 99 base 10 to hex

First convert to binary:



Then binary to hex:

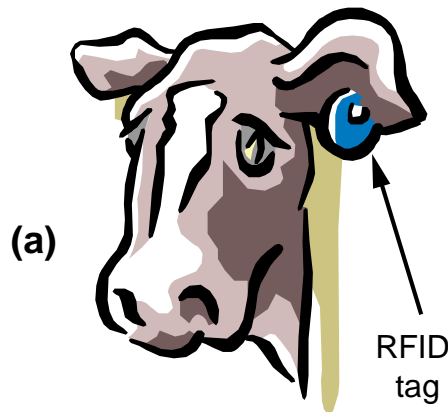


(Quick check: $6*16 + 3*1 = 96+3 = 99$) *a*



Hex Example: RFID Tag

- Batteryless tag powered by radio field
 - Transmits unique identification number
 - Example: 32 bit id
 - 8-bit province number, 8-bit country number, 16-bit animal number
 - Tag contents are in binary
 - But programmers use hex when writing/reading



(c) Province: 7 City: 160 Animal: 513

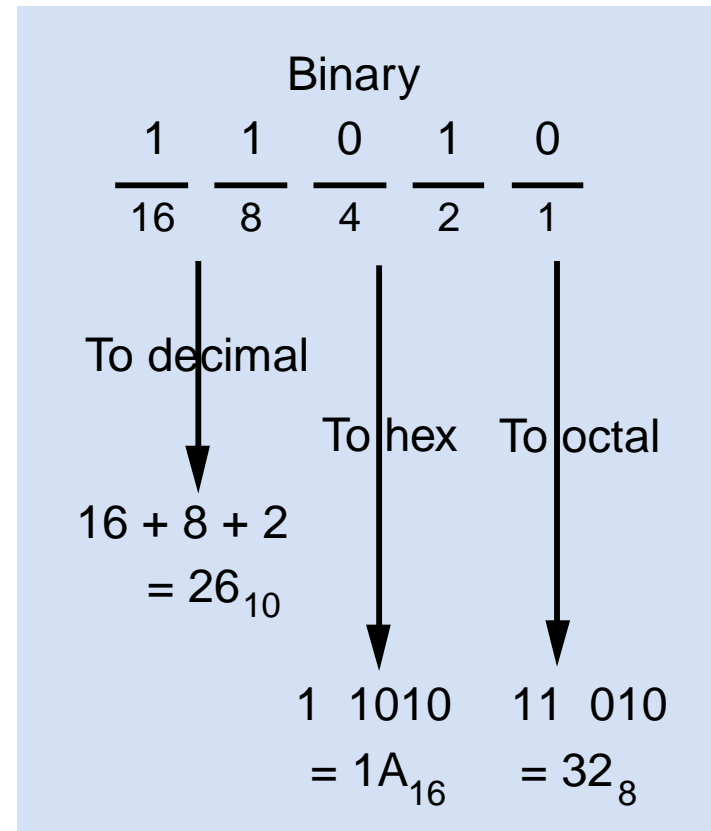
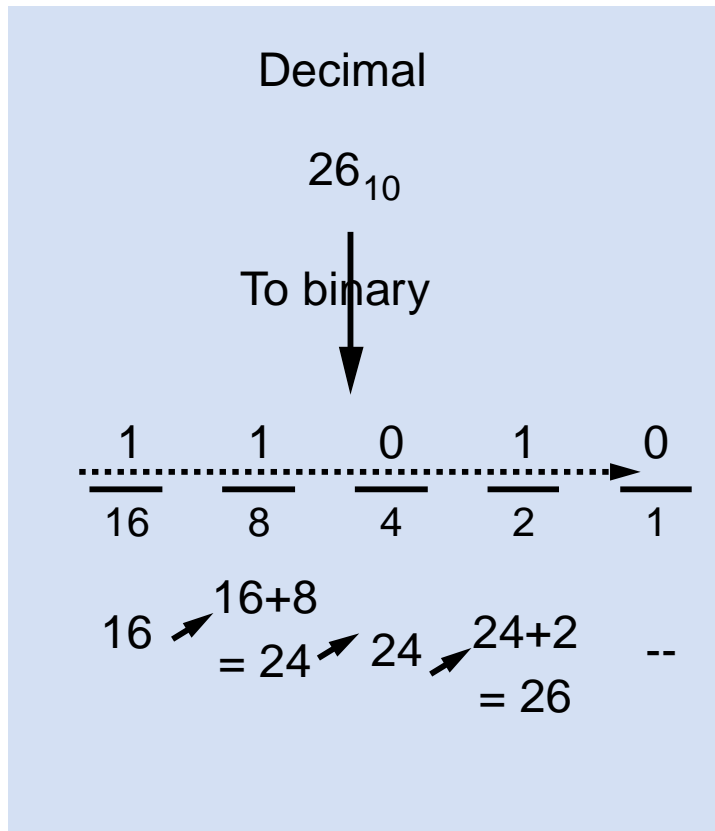
(d) 00000111 10100000 00000010 00000001

(e) 07 A0 02 01

(f) **Tag ID in hex: 07A00201**



Converting To/From Binary by Hand: Summary



Divide-By-2 Method Common in Automatic Conversion


- Repeatedly divide decimal number by 2, place remainder in current binary digit (starting from 1s column)

	<u>Decimal</u>	<u>Binary</u>
1. Divide decimal number by 2 Insert remainder into the binary number Continue since quotient (6) is greater than 0	$\begin{array}{r} 6 \\ 2\sqrt{12} \\ -12 \\ \hline 0 \end{array}$	$\frac{0}{1}$ <i>(current value: 0)</i>
2. Divide quotient by 2 Insert remainder into the binary number Continue since quotient (3) is greater than 0	$\begin{array}{r} 3 \\ 2\sqrt{6} \\ -6 \\ \hline 0 \end{array}$	$\frac{0}{2} \frac{0}{1}$ <i>(current value: 0)</i>
3. Divide quotient by 2 Insert remainder into the binary number Continue since quotient (1) is greater than 0	$\begin{array}{r} 1 \\ 2\sqrt{3} \\ -2 \\ \hline 1 \end{array}$	$\frac{1}{4} \frac{0}{2} \frac{0}{1}$ <i>(current value: 4)</i>
4. Divide quotient by 2 Insert remainder into the binary number Quotient is 0, done	$\begin{array}{r} 0 \\ 2\sqrt{1} \\ -0 \\ \hline 1 \end{array}$	$\frac{1}{8} \frac{1}{4} \frac{0}{2} \frac{0}{1}$ <i>(current value: 12)</i>

*Note:
Works for
any base
N—just
divide by
N instead*



Bytes, Kilobytes, Megabytes, and More

- Byte: 8 bits 
- Common metric prefixes:
 - kilo (thousand, or 10^3), mega (million, or 10^6), giga (billion, or 10^9), and tera (trillion, or 10^{12}), e.g., kilobyte, or KByte
- BUT, metric prefixes also commonly used inaccurately
 - $2^{16} = 65536$ commonly written as “64 Kbyte”
 - Typical when describing memory sizes
- Also watch out for “KB” for kilobyte vs. “Kb” for kilobit



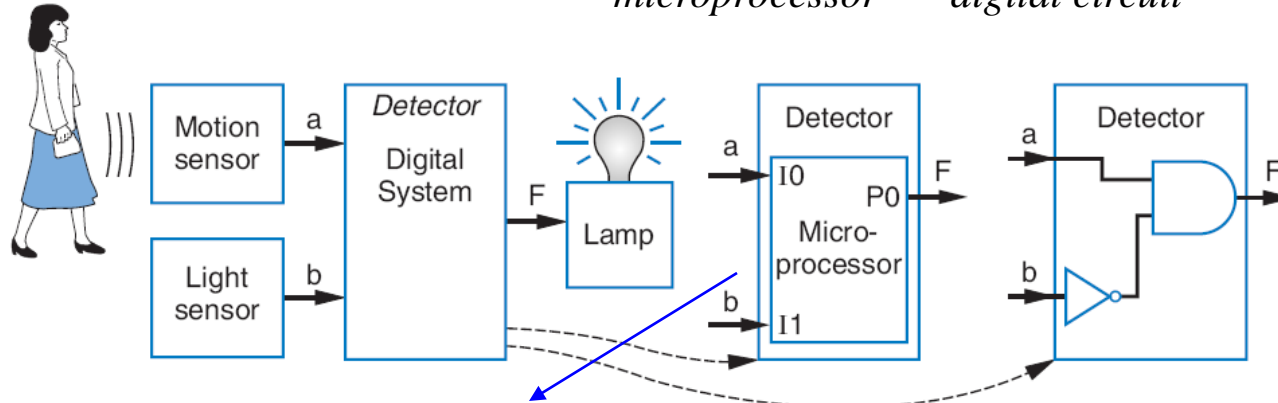
Implementing Digital Systems: Programming Microprocessors Vs. Designing Digital Circuits

Desired motion-at-night detector

Programmed microprocessor

Custom designed digital circuit

- Microprocessors a common choice to implement a digital system
 - Easy to program
 - Cheap (as low as \$1)
 - Readily available



—	I0	P0	—
—	I1	P1	—
—	I2	P2	—
—	I3	P3	—
—	I4	P4	—
—	I5	P5	—
—	I6	P6	—
—	I7	P7	—

```

void main()
{
    while (1) {
        P0 = I0 && !I1;
        // F = a and !b,
    }
}
        
```

Digital Design: When Microprocessors Aren't Good Enough

- With microprocessors so easy, cheap, and available, why design a digital circuit?
 - Microprocessor may be too slow
 - Or too big, power hungry, or costly



Wing controller computation task:

- 50 ms on microprocessor
- 5 ms as custom digital circuit

If must execute 100 times per second:

- $100 * 50 \text{ ms} = 5000 \text{ ms} = 5 \text{ seconds}$
- $100 * 5 \text{ ms} = 500 \text{ ms} = 0.5 \text{ seconds}$

Microprocessor too slow, circuit OK.

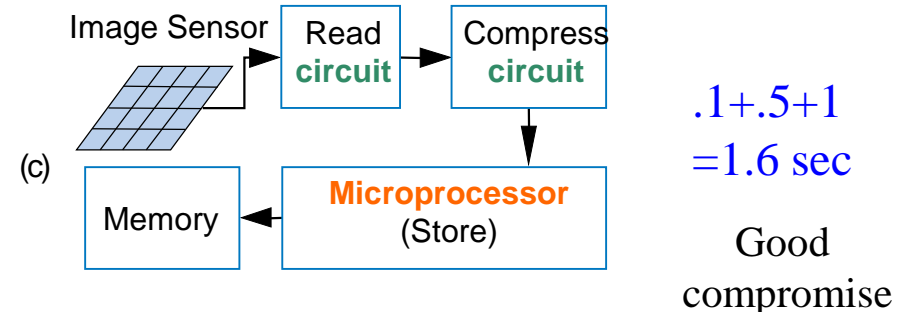
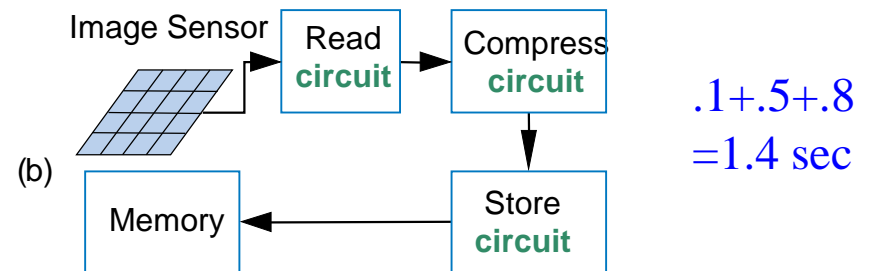
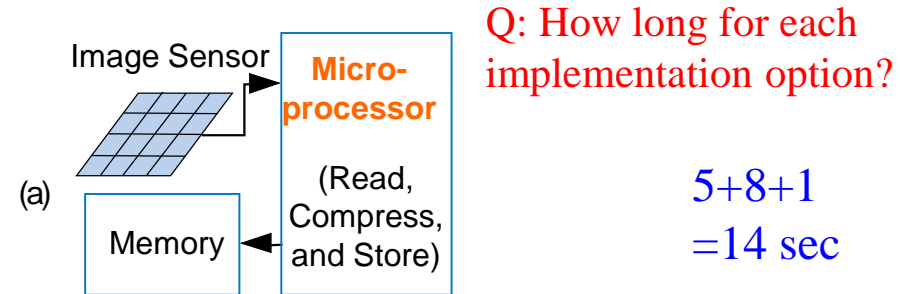


Digital Design: When Microprocessors Aren't Good Enough

- Commonly, designers partition a system among a microprocessor and custom digital circuits

Sample digital camera task execution times (in seconds) on a microprocessor versus a digital circuit:

Task	Microprocessor	Custom Digital Circuit
Read	5	0.1
Compress	8	0.5
Store	1	0.8



Chapter Summary

- Digital systems surround us
 - Inside computers
 - Inside many other electronic devices (embedded systems)
- Digital systems use 0s and 1s
 - Encoding analog signals to digital can provide many benefits
 - e.g., audio—higher-quality storage/transmission, compression, etc.
 - Encoding integers as 0s and 1s: Binary numbers
- Microprocessors (themselves digital) can implement many digital systems easily and inexpensively
 - But often not good enough—need custom digital circuits

