

CORDIC: An Efficient Trigonometric Algorithm for Embedded Systems

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Introduction

- CORDIC, is an acronym for **CO**ordinate **R**otation **D**igital **C**omputer.
- These algorithms are a class of iterative solutions for trigonometric and other transcendental functions that use only shifts and adds.
- The trigonometric functions are based on vector rotations.

Introduction Cont'd....

The CORDIC algorithm has found its way into diverse applications,

- Ø 8087 math coprocessor ,
- Ø The HP-35 calculator,
- Ø Radar signal processors,
- Ø Robotics,
- Ø Computing Discrete Fourier,
- Ø Discrete Cosine,
- Ø Discrete Hartley and Chirp-Z Transforms,
- Ø Filtering.

CORDIC THEORY

A general rotation transformation is given as,

$$\begin{aligned}x' &= x \cos \phi - y \sin \phi \\y' &= y \cos \phi + x \sin \phi\end{aligned}$$

Which rotates a vector in a cartesian plane by the angle Φ ,

$$\begin{aligned}x' &= \cos \phi \cdot [x - y \tan \phi] \\y' &= \cos \phi \cdot [y + x \tan \phi]\end{aligned}$$

Taking $\Phi = 2^{-i}$, we get,

$$\begin{aligned}x_{i+1} &= K_i [x_i - y_i \cdot d_i \cdot 2^{-i}] \\y_{i+1} &= K_i [y_i + x_i \cdot d_i \cdot 2^{-i}]\end{aligned}$$

where:

$$\begin{aligned}K_i &= \cos(\tan^{-1} 2^{-i}) = 1/\sqrt{1+2^{-2i}} \\d_i &= \pm 1\end{aligned}$$

CORDIC THEORY Cont'd....

The factor A_n , can be used to start of the iteration.

$$A_n = \prod_n \sqrt{1+2^{-2i}}$$

$$x_{i+1} = x_i - y_i \cdot d_i \cdot 2^{-i}$$

$$y_{i+1} = y_i + x_i \cdot d_i \cdot 2^{-i}$$

$$z_{i+1} = z_i - d_i \cdot \tan^{-1}(2^{-i})$$

where

$$d_i = -1 \text{ if } z_i < 0, +1 \text{ otherwise}$$

CORDIC THEORY Cont'd....

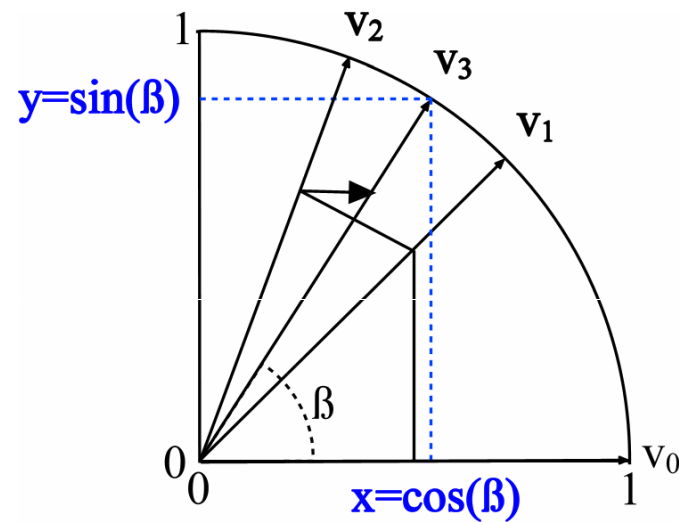


Figure 1: Step by step iteration

Hardware Block Diagram

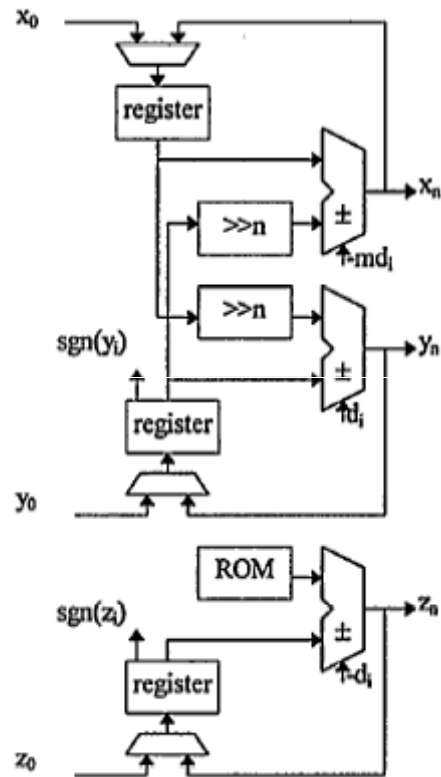


Figure 2: Iterative CORDIC Structure

Code Stamps on a Renesas MC62P

With Math Library

| | |
|---------|-------------------------|
| DATA | 0002424(00978H) Byte(s) |
| ROMDATA | 0000418(001A2H) Byte(s) |
| CODE | 0008416(020E0H) Byte(s) |

CORDIC Implementation

| | |
|---------|-------------------------|
| DATA | 0002880(00B40H) Byte(s) |
| ROMDATA | 0000404(00194H) Byte(s) |
| CODE | 0003273(00CC9H) Byte(s) |

Pros and Cons

- CORDIC is an iterative based approach with just shifts, adds and table look-up.
- It is commonly used when no hardware multiplier is available.
- CORDIC is particularly well-suited for handheld calculators, an application for which cost (i.e., chip gate count has to be minimized) is much more important than is speed

Pros and Cons Cont'd

When a hardware multiplier is available (e.g. in a DSP microprocessor), table-lookup methods and power series are generally faster than CORDIC.