

Homework Set 11

Basic Limits

(sect 1.4, 1.6, 3.1 – 3.2)

Use an appropriate rule to compute the following limits.

1.

$$\lim_{x \rightarrow \infty} \frac{1}{x^{5/2}} = 0$$

2.

$$\lim_{x \rightarrow \infty} \left(\frac{1}{3}\right)^x = 0$$

3.

$$\lim_{x \rightarrow 0} \frac{x}{\sin x} = 1$$

4.

$$\lim_{x \rightarrow -\infty} \arctan x = -\pi/2$$

5.

$$\lim_{x \rightarrow \infty} \ln(x^3) = \infty$$

6.

$$\lim_{x \rightarrow \infty} e^{-2x} = 0$$

7.

$$\lim_{x \rightarrow 7} 53 = 53$$

8.

$$\lim_{x \rightarrow 1} \ln x = 0$$

9.

$$\lim_{x \rightarrow \infty} \left(\frac{9}{10}\right)^{-x} = \infty$$

10.

$$\begin{aligned} \lim_{x \rightarrow 0} \frac{\tan 2x}{3x} &= \lim_{x \rightarrow 0} \frac{\sin 2x}{3x \cos 2x} = \lim_{x \rightarrow 0} \left(\frac{\sin 2x}{2x} \cdot \frac{2}{3 \cos 2x} \right) \\ &= 1 \cdot \lim_{x \rightarrow 0} \frac{2}{3 \cos 2x} = \frac{2}{3 \cos 0} = \frac{2}{3} \end{aligned}$$