

QUIZ 10

1. (8 points) Which of the following integrals are improper? If an integral is improper, identify what makes it improper.

$$\int_{-1}^1 \frac{1}{x^5} dx \quad \begin{array}{l} \text{improper} \\ x \neq 0 \end{array}$$

$$\int_4^{\infty} 3e^{-x/2} dx \quad \begin{array}{l} \text{improper} \\ x \neq \infty \end{array}$$

$$\int_0^{\pi/4} \frac{5}{1 - \sin x} dx \quad \text{not improper}$$

$$\int_0^1 \frac{4x}{\sqrt{x^2 - 1}} dx \quad \begin{array}{l} \text{improper} \\ x \neq 1 \end{array}$$

2. (2 points) Does the following integral converge or diverge?

$$\begin{aligned} & \int_1^{\infty} \frac{1}{x\sqrt{x}} dx \\ &= \lim_{t \rightarrow \infty} \int_1^t x^{-3/2} dx \\ &= \lim_{t \rightarrow \infty} \left. -2x^{-1/2} \right|_1^t \\ &= \lim_{t \rightarrow \infty} \left[\frac{-2}{\sqrt{t}} + \frac{2}{\sqrt{1}} \right] \\ &= 0 + 2 \\ &= 2 \end{aligned}$$