

QUIZ 1

1. (2 points) Simplify: $2 + \frac{x}{\left(\frac{3}{x+1}\right)}$

$$= 2 + \frac{x}{1} \cdot \frac{x+1}{3} = 2 + \frac{x^2+x}{3} = \frac{6}{3} + \frac{x^2+x}{3} = \frac{x^2+x+6}{3}$$

2. (2 points) Factor: $x^4 - x^3 - 6x^2$

$$= x^2(x^2 - x - 6) = x^2(x - 3)(x + 2)$$

3. (2 points) Match the radian measurement of the angle to its corresponding degree measurement.

- a. $\frac{\pi}{2}$ ~~30°~~
- b. $\frac{\pi}{6}$ ~~135°~~
- c. $\frac{3\pi}{4}$ ~~60°~~
- d. $\frac{\pi}{3}$ ~~90°~~

4. (4 points) Find the 2nd derivative of $f(x) = \arctan(2x)$. (Recall, that $\arctan(u) = \tan^{-1}(u)$.)

$$f'(x) = \frac{1}{(2x)^2 + 1} \cdot \frac{d}{dx}(2x) = \frac{2}{4x^2 + 1} \quad \text{OR} \quad 2(4x^2 + 1)^{-1}$$

$$f''(x) = 2(-1)(4x^2 + 1)^{-1-1} \cdot \frac{d}{dx}(4x^2 + 1) = -2(4x^2 + 1)^{-2} \cdot 8x = -16x(4x^2 + 1)^{-2}$$

OR

$$f''(x) = \frac{(0)(4x^2 + 1) - (2)(8x)}{(4x^2 + 1)^2} = -\frac{16x}{(4x^2 + 1)^2}$$