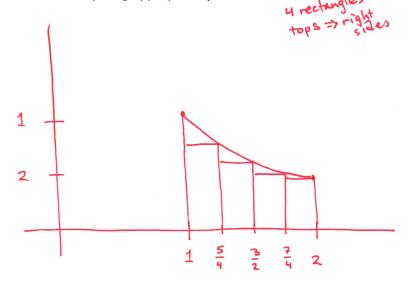
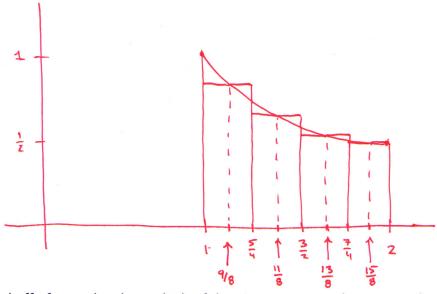
Consider the function  $f(x) = \frac{1}{x}$  on the interval x = 1 to x = 2.

1. (5 points) Sketch a diagram of its right Riemann sum  $R_4$ , and find  $\Delta x$  for this Riemann sum. Be sure to label everything appropriately.



 $\Delta x = \frac{b-a}{n} = \frac{2-1}{4} = \frac{1}{4}$ 

2. (3 points) Sketch a diagram of the Riemann sum  $M_4$  (called the midpoint rule).



3. (2 points) Based off of your sketches, which of the Riemann sums above gives the most accurate estimate of the area between the lines  $f(x) = \frac{1}{x}$ , x = 1, x = 2, and the x-axis?

the midpoint rule