

QUIZ 4

1. (3 points) Rewrite the following limit on $[1,4]$ as a definite integral:

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n [x_i \tan 3x_i] \Delta x$$

$$= \int_1^4 x \tan(3x) dx$$

2. (3 points) Consider $\int_0^2 (6x - 1) dx$. Suppose that you want to compute this definite integral using the definition (ie: finding the limit of the Riemann sum). Find Δx and x_i for this definite integral.

$$\Delta x = \frac{b - a}{n} = \frac{2 - 0}{n} = \frac{2}{n}$$

$$x_i = a + i\Delta x = 0 + i \cdot \frac{2}{n} = \frac{2i}{n}$$

3. (4 points) Compute $\int_0^2 (6x - 1) dx$.

$$= 3x^2 - x \Big|_0^2 = (12 - 2) - (0) = 10$$

Or you can use Riemann Sums or draw a picture and compute the area of the triangles. The above way of using antiderivatives is the quickest.